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COMPUTER MODILING OF THIN FILM GROWTH HERSIS

Jeifrey A. Stefeneck Captain, MSAR

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THESIS

Jeffrey A. Stefoneck Captain, USAF

AFIT/GEP/PH/84D-10



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COMPUTER MODELING OF THIN FILM GROWTH

THESIS

Presented to the Faculty of the School of Engineering
of the Air Force Institute of Technology
Air University
In Partial Fulfillment of the
Requirements for the Degree of
Master of Science in Engineering Physics

Jeffrey A. Stefoneck, B.S.

Captain, USAF

December 1984

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Preface

This study represents an initial effort to give the Air Force Institute of Technology (AFIT) a computer model which simulates thin film growth by vapor-deposition. It was my goal in this effort to establish an initial building block which follow on studies could use to expand and modify. It is my hope that with this documentation and programming, modification and expansion will be a relatively easy task.

Finally, a word of thanks to all of the AFIT Faculty who provided guidance in this effort, especially Major Wharton. Also, I wish to thank my wife Debra for her understanding, concern, and typing, and my sons Brian and Aaron for the guiet hours they gave.

Jeffrey A. Stefoneck

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Abstract

Made which simulates thin film growth. The model represents deposition molecules by hard disks, which are trajected at some angle to the substrate. At the substrate, the model assumes a limited mobility where incident molecules are captured upon contact and then allowed to move to the nearest rest pocket. The model monitors disk movement by organizing the deposition field into a 320 by 240 array.

An analysis of nine different deposition angles shows that structural anisotropy and voids are a natural occurrence of the deposition process. The amount of unfilled space and the anisotropy can be linked to the deposition angle and mobility of the incident particles.

COMPUTER SIMULATION OF VAPOR DEPOSITED THIN FILM GROWTH

I. Introduction

Vapor-deposited thin films play important roles in many technologies, most notably in optics and microelectronics. In optics, thin films are commonly used for anti-reflection coatings and in broad and narrow band-pass filters. The application of thin film optical devices are manifold, as are their structures, which extend from the simplest single coatings to intricate arrangements of 100 or more layers. In microelectronics, thin films also play an important role. Integrated circuit electronics technology, for example, relies heavily upon vapor-deposited thin films for the formation of metal interconnections.

One technique used for producing thin films is vapordeposition. In this method, a small quantity of material is
placed inside a vacuum chamber where it is heated and the
surrounding pressure is lowered to a millionth of atmospheric
pressure or less. In addition, the vacuum chamber contains a
substrate where the temperature is held equal to or less than
half the melting point temperature of the material to be
deposited. Thus, the material is evaporated and condenses
onto the substrate where a thin film is produced.

Crystalline and amorphous thin films produced by this kind of deposition commonly exhibit excess volume. This

volume, in the form of lattice vacancies, pores, and voids is a nearly universal feature of vapor-deposited thin films. The microstructure formed is columnar as observed by microfractography [Ref 5-9, 12, 18, 19]; by transmission electron microscopy [Ref 4, 9, 14-16, 21, 24, 25]; and by small angle electron [Ref 9, 16, 24, 25] and x-ray scattering [Ref 2, 13, 23], and at large scattering angles in amorphous films [Ref 21, 23]. In addition, the formation of the columnar microstructure has been found to depend upon deposition conditions -- substrate temperature, deposition rate, angle of incidence, and vacuum ambient -- as well as upon the material.

The physical properties of vapor-deposited thin films differ greatly from those of bulk material. Magnetic, optical, electrical, and mechanical properties are known to be influenced by the presence of the columnar structure [Ref 10]. In addition, the columnar microstructure, and thereby the physical properties, can be varied through the deposition conditions. Due to this variability in physical properties, thin films are playing an ever increasing role in optics and microelectronics.

Purpose of Study

The purpose of this study was to make a computer simulation of the vapor-deposition process in such a way as to give rise to an amorphous array of molecules with demonstrable anisotropy and void formations.

Assumptions

In this study, various assumptions were made. The most general are presented here. A more complete list and discussion of their reasonability are presented in Chapter II.

- 1. It is assumed that the physical thin film deposition process can adequately be represented by a twodimensional model.
- 2. Each particle (atom, molecule, or collection of molecules) is assumed to travel on a straight line and at an angle A from the substrate normal until it comes in contact with one of the already deposited particles or substrate.
- 3. It is assumed that the temperature of the substrate or film and the energy of the incoming particles are such that once they contact a particle (substrate or film), they will stick. Furthermore, the incident particle is assumed always to remain in contact with the particle with which it first made contact. However, the incident particle is allowed to relax to the extent that it moves about the perimeter of the contacted particle until it makes contact with the next closest particle (substrate or film).

General Approach

This study was conducted in eight separate steps: model definition, assumption identification, scope definition,

mathematical model development, program development, program testing, simulation activation, and results analysis. In general, the order of implementation was the same. However, as in most studies, some problems encountered required taking a step or two backwards and reaccomplishing them.

Summary of Current Knowledge

Several properties of thin film columnar growth have been observed and can be used to verify theoretical results. First, for oblique incidence deposition, the columns are found to be inclined toward the vapor source and form an angle B with the substrate normal (See Figure 1.1). The angle formed by the vapor beam and substrate normal is A and is related to B by

2 an B = an A, which has become known as the Tangent Rule [Ref 17].

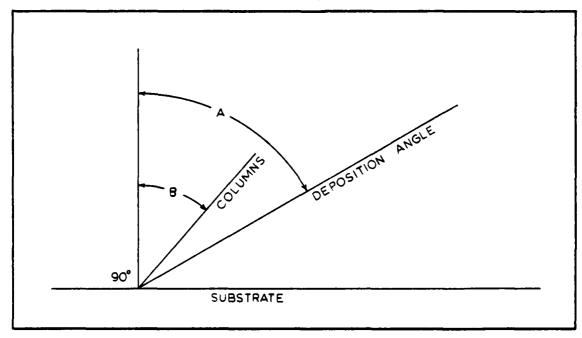


Fig. 1.1 Angles of Tangent Rule

Second, oblique incidence deposition is often accompanied by a change in column shape. While the columnar cross section of normally deposited films are invariably equiaxed, oblique deposition yields columns that are elongated in the direction perpendicular to the plane of incidence (plane determined by the vapor beam and foil normal). Third, although more prominent in obliquely deposited films, the columnar structure persists under conditions of normal incidence deposition. Finally, an increase in A leads to an increase in the spacing between columns and a decrease in the frequency of column branching.

Sequence of Presentation

The results of this study will be presented in the five remaining chapters and two appendixes. In Chapter II, current literature will be reviewed and a physical model developed. Then some simplifying assumptions will be made and the resulting computer model presented. Chapter III will present the computer program and how the model is implemented, while Chapter IV will discuss the computer program validation. Chapter V will show the results of some simulation runs along with their analysis. All conclusions and recommendations will be presented in Chapter VI. The appendixes contain two types of information which are of great importance to follow on studies but is of little use to the casual reader. Appendix A contains the complete Fortran listing of the computer program with all of the built-in self testing procedures.

Appendix B contains various derivations. Since most derivations concerning this simulation are common algebra derivations, they were put in the appendixes for those people that wish to be reacquainted with them.

II Analysis

The purpose of this study was to make a computer simulation of the vapor-deposition process in such a way as to give rise to an amorphous array of molecules with demonstrable anisotropy and void formations. To accomplish this goal, an adequate model of the physical process needed to be constructed. This was carried out in three phases. The first was a literature search for any applicable experimental results or observations. Then the data collected was analyzed and some assumptions were made. Finally, the model was constructed. The applicable portions of these phases are presented in capsulized form in the remainder of this chapter.

Applicable Experimental Results and Observations

Crystalline and amorphous thin films produced by vapor deposition commonly exhibit a columnar microstructure and excess volume. The volume, in the form of lattice vacancies, pores, and voids is a nearly universal feature. The microstructure formed is columnar as observed by microfractography [Ref 5-9, 12, 18, 19]; by transmission electron microscopy [Ref 4, 9, 14-16, 21, 24, 25]; and by small angle electron [Ref 9, 16, 24, 25] and x-ray scattering [Ref 2, 13, 23], and at large scattering angles in amorphous films [Ref 21, 23]. One example of the columnar microstructure is that revealed by Nieuwenhuizen and Haanstra [Ref 17] by microfractography. Figure 2.1 shows one of their fractographs of the structure

in an aluminum film that was produced by oblique incidence deposition in a 10^{-5} Torr atmosphere.

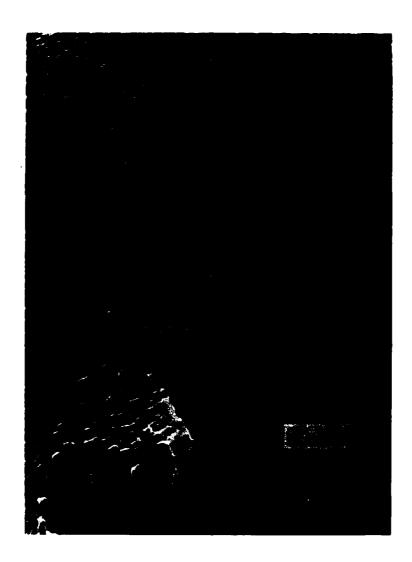


Fig. 2.1. Microfractograph [Ref 17] of Fractured Edge of lµm thick Al Film

The angle at which these columns grow has also been studied. Nieuwenhuizen and Haanstra [Ref 17] first reported careful determinations of this over a wide range of deposi-

tion angles and found that their results could be well described by what has become known as the "tangent rule".

$2 \tan B = \tan A$

Here B is the angle formed between the column growth and the substrate normal, and A is the angle formed between the source direction and the substrate normal (See Figure 2.2a). Figure 2.2b shows the columnar growth angle versus deposition angle as a result of the tangent rule, and as a result of a columnar growth angle equal to the deposition angle (a common misconception).

Although the tangent rule was obtained by experimental observation, much data has been accumulated to support it in general. Leamy et al [Ref 10:317] has compiled data from many sources on depositions of crystalline and amorphous thin films, and has found that the tangent rule was obeyed by all data considered at $0^{\circ} \leq A \leq 60^{\circ}$. In fact, only the results of Nakhodkin and Shaldervan at $A > 60^{\circ}$ does not fall within acceptable ranges of the tangent rule. However, in recent years some experimentalists have found that the tangent rule may not apply under certain conditions [Ref 10].

In conjunction with studies on columnar growth angle, Nakhodkin and Shaldervan [Ref 15:22-24] have noted that the formation of columns depend upon the deposition conditions (substrate temperature, deposition rate, angle of incidence and vacuum ambient) as well as upon the material itself. Leamy et al [Ref 10:312] have noted from source considered, that columnar structures were observed only when the mobility

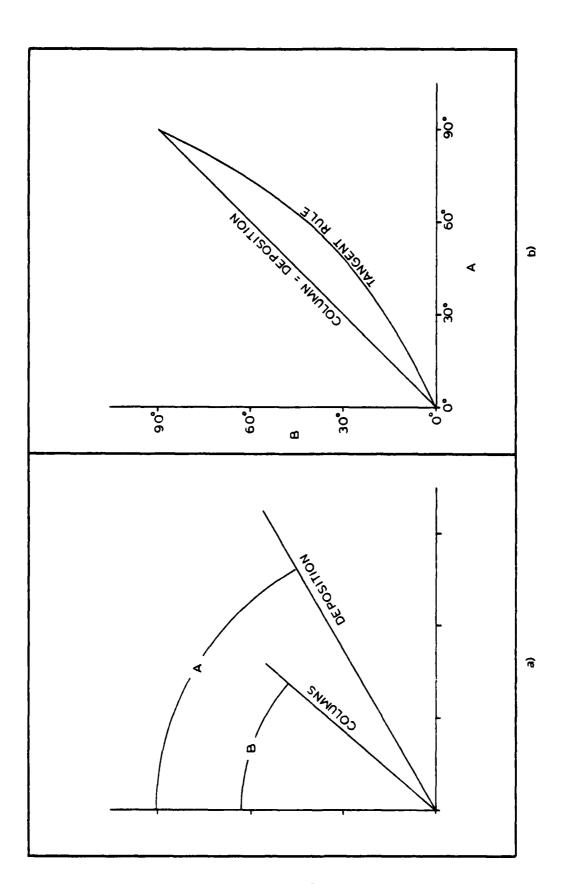


Fig. 2.2. Tangent Rule

(capability of the particles to move once attached to the substrate or film) of the deposited atoms were "limited". For example, columns are observed in films of high melting point materials (chromium, beryllium, silicon and germanium), in compound materials of high binding energy (CdTe, CAF2, and PbS), and in non-noble metals evaporated in the presence of oxygen (aluminum, iron, and N_1 -Fe). Amorphous films (silicon, germanium, S_1 0, and RE-TM alloys), whose existence in the amorphous state depends upon a limited atomic mobility, universally exhibit a columnar structure when deposited at sufficiently low temperatures. It has also been noted that depositions with successively increasing substrate temperatures eventually lead to the elimination of the columnar structure [Ref 10:317].

In addition to the angle of the columnar microstructure and a limited mobility, other characteristics have also been found. For example, oblique incidence deposition is often accompanied by a change in column shape. While the columnar cross section of normally deposited films are invariably equiaxed, oblique deposition yields columns that are elongated in the direction perpendicular to the plane of incidence (plane determined by the vapor beam and the foil normal) [Ref 10:13]. As angle of incidence increases, the column shape becomes more elliptical and the void regions between columns become thinner along a direction parallel to the incidence direction. This increase in void network size is reflected in density measurements, which show a monotonic

decrease in density with increasing A [Ref 15:24, 21]. Finally, although more prominent in obliquely deposited films, the columnar structure persists under conditions of normal incidence deposition [Ref 9, 15, 16].

Mobility and Shadowing

In vapor deposition, direct condensation of vapor atoms occurs on substrates at temperatures equal to or less than half the melting point temperature of the vapor species. This causes vapor-solid reactions to proceed under highly nonequilibrium conditions. Consequently, the rate for evaporation is insignificant relative to the rate of condensation. Therefore, for the sake of simplicity, it could be assumed without unreasonable error that incoming particles are captured by the substrate at first impact.

After the particle is captured by the substrate, whether on the first or whatever encounter, another question needs to be answered. How much can the particle move on the substrate before settling? Does it have an infinite, low, or no mobility? Consider first the case of infinite substrate mobility. In this case, a uniform type of material would be formed. Similar to marbles in a box, a dense pack configuration results. A crude example of this would be the formation of solids by the freezing of liquids. The last case, of no substrate mobility, produces results just as unacceptable. Here the columnar structure is formed, but the chainlike structure formed would produce a material density which would

be unrealistic. This leaves only the case of low or limited mobility as an acceptable possibility. Also this bears out Nakhodkin and Heinemann's observation that columnar structures are possible only when the mobility of deposited atoms were limited.

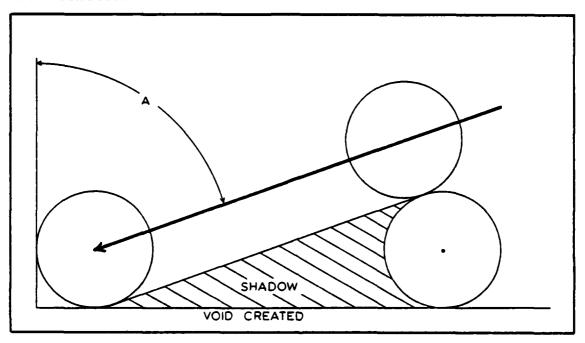


Fig. 2.3. Particle Shadowing

If limited mobility is assumed, the formation of voids can be understood with little difficulty. Consider the finite size particles shown in Figure 2.3. Particle x represents a substrate protrusion. If particle y was trajected to the left of particle x with a trajectory angle of A, the closest that it could impact would be some distance away. In other words, the substrate particles that are directly exposed to the vapor beam shield or shadow unoccupied sites. Thus voids are created. If migration of the particles after condensation does not fill up the voids (limited mobility),

the void structure is maintained and grows with the subsequent deposition of particles.

The consequences of shadowing and limited mobility also produce other effects which have been noted in experimental results. One case in point is the decrease in density experienced with increasing A [Ref 15:24, 21]. It is easy to see from Figure 2.3, that an increase in A would also increase the void width and therefore would decrease the density.

A Model of the Thin Film Growth Process

Thin film growth by vapor-deposition can be pictured quite accurately in light of the previous section. The process is described here in the sequential order that a particle being deposited would see it.

In the vapor-deposition process, particles (atoms, molecules, or collection of molecules) are ejected at a point above the substrate with some determined rate and angle A from the substrate normal. Each particle moves thermodynamically. As a whole, the particles comprise a vapor beam which moves at angle A toward the substrate. After traveling for some time, particles of the vapor beam encounter the substrate. Whether they attach themselves, bounce, attach and release again, etc. is determined by the energies of the incoming particle and the substrate particles contacted. Once the particle is attached to the substrate, the particle is permitted to move on the substrate. However, the movement of the particle on the substrate is limited. How limited

again depends on the energy that the particle still possesses and the energies of the substrate particles on which it encounters. Eventually, the particle becomes affixed to the substrate. As more and more particles attach themselves to the substrate and settle, the film grows.

Computer Model

In an attempt to build a starting block computer model, many assumptions need to be made and justified. Once this is done a more simplified model can be constructed. In this section, all assumptions will be presented along with a short justification and the ensuing computer model described.

- 1. It is assumed that the thin film deposition process can adequately be represented by a two dimensional model. -- This assumption is reasonable since most quantities desired happen in a plane determined by the substrate normal and the vapor beam. Shape of the columnar growth is the exception.
- 2. The incident particles are assumed to be disks of a constant diameter D. -- Experimental results of many different substances yield similar microstructures, and therefore suggest that shape does not play an important role in thin film growth.
- 3. The rate at which particles are ejected from the vapor beam source is small enough that they can be considered as serial events. -- If the mean free path and arrival rate of the ejected particles are

calculated as described in Reference 1, it is easy to see that interaction of incoming particles is rare. Thus the particles can be considered one at a time without any real problem with particle interaction.

- 4. Each particle is assumed to travel on a straight line and at an angle A from the substrate normal until it comes in contact with the substrate or one of the already deposited particles. -- Again, if the mean free path of the vapor particles is calculated as described in Reference 1, it is easy to see that interaction is rare and travel should be in a straight line. In addition, if the impact points are chosen randomly in the model, this should introduce little error.
- or film and the energy of the incoming particles are such that once they contact a particle (substrate or film), they will stick. Furthermore, limited mobility is assumed; the incident particle always remains in contact with the particle with which it first made contact, however, it is allowed to relax by moving around the perimeter of the contacted particle until it makes contact with the next closest particle (substrate or film). The reasonability of this assumption was discussed previously in the section on mobility and shadowing.

Simplified Computer Model

In the computer model of the vapor deposition process, disks are trajected serially in a straight line to the substrate at angle A from the substrate normal. The x axis start point of each disk trajectory is randomly selected. When an incoming disk makes contact with a substrate disk they stick. The incoming disk then moves around the perimeter of the contact disk until it contacts the next closest disk (substrate or film). Finally, the movement of that incoming disk becomes restricted after two contacts are made, and the process starts over again with another disk being trajected.

III Thin Film Growth (TFG) Simulator

A computer simulation of TFG requires the ability to perform at least two tasks. Obviously one task is to simulate the deposition process. The second is a prerequisite required for the deposition process to occur. It is the task of providing a substrate (a collection of particles on which incident molecules or atoms come to rest). If a substrate is provided and the deposition process can be simulated, the basic ingredients for a TFG simulator are at hand.

In addition to the basic requirements for TFG simulation, analysis programs or methods must also be available if a TFG simulation is to be useful. Exactly what the analysis programs or methods consist of are determined by the information sought. In this particular case, the structure of the thin film is of interest. More specifically, this analysis consists of getting the density, the angle of columnar growth, and a graphic representation of the thin film. The simulator must then contain the ability to perform the basic requirement of TFG simulation and the required analysis.

The TFG simulator, as presented in Appendix A, has the ability to do four of the five tasks mentioned above. It can provide substrates, simulate deposition, calculate density, and solve for the angle of columnar growth. Since software is available that will give a graphic representation of particle locations, this feature was not included. However, the TFG simulator presented in Appendix A together with S (a

statistical and graphics system from Bell Laboratories) satisfies all the requirements established.

The TFG simulator program is composed of a main program interface loop and four subprograms; the buffer editor, the matrix manager, the TFG depositor, and the analyzer. Functionally, the TFG simulator has only three parts: the substrate builder, the TFG depositor, and TFG analyzer. This structure and program control flow is shown in Figure 3.1.

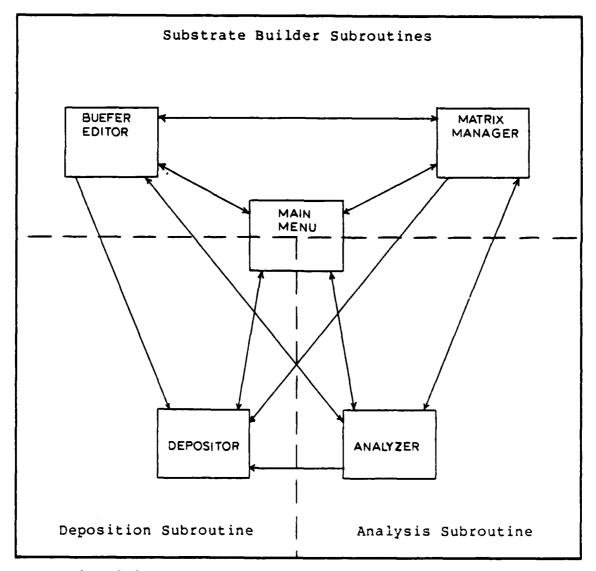


Fig. 3.1. TFG Structure and Program Control Flow

Substrate Handler

The substrate handler provides the TFG simulator the ability to create, modify, store, and recall substrates. It is formed from two TFG simulator subprograms; the buffer editor and the matrix manager. The ability for it to store or recall substrates comes from the matrix manager, whereas the ability for it to create or modify substrates arises through the combined effort of the buffer editor and the matrix manager.

The buffer editor is a convenience interface subprogram. It allows for direct human interface by providing a 240 line buffer which can be filled with substrate building commands. This thereby relieves the user of entering the location of every particle in the substrate. For example, a flat substrate may consist of several hundred particles. The buffer editor provides a means of describing the location of all these particles with just two short line commands of usually less than 25 keystrokes.

The matrix manager provides user control of matrix size and data transfers in or out of the simulator. This is accomplished by several user selectable matrix manager subprograms. The set axes subprogram can set the xy field matrix to 320x240, 160x120, or 80x60 unit cells. Data transfers are accomplished by the read/write subprograms which read and write external field and substrate files. In addition, matrix manager subprograms do all calculations necessary to convert buffer commands to disk locations, which can

then be added to, deleted from, or be entered for the first time into the xy field matrix.

The substrate handler theory of operation is quite simple. It assumes that any given two-dimensional substrate can be represented by a series of single disks, line of disks, or any combination thereof. Examples of these are shown in Figure 3.2. Single disks are entered into the buffer by entering its x and y coordinates. A line of N disks is entered as a length of N disks and a standard angle from the positive x axis as shown in Figure 3.3. The starting point of each line is the last point or the last point of the last line entered. For example, the line in Figure 3.3 could be entered through the buffer by first specifying disk 1 and then specifying the remaining segment. These two buffer commands are listed in the figure.

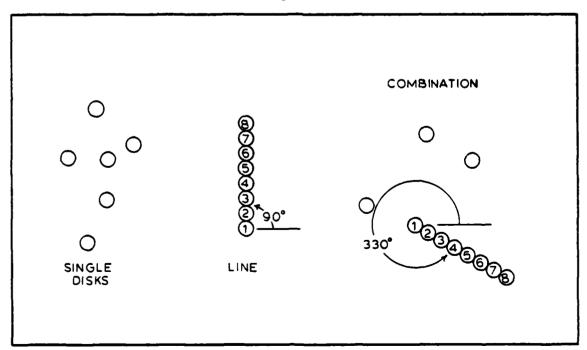


Fig. 3.2. Two Dimensional Substrate Examples

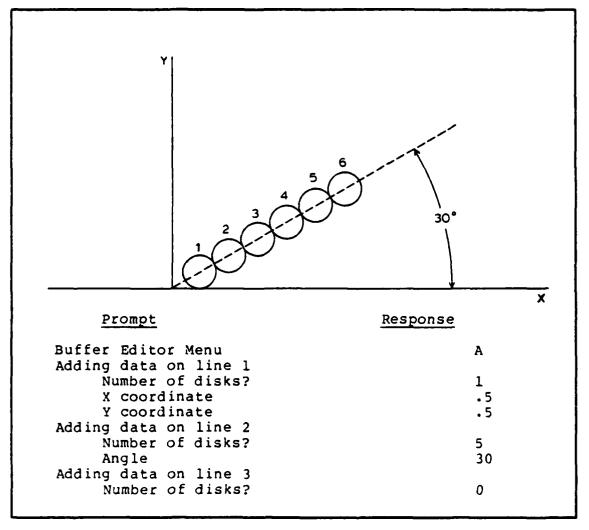


Fig. 3.3. Line Substrate with Appropriate Buffer Commands

After the data is entered in the buffer, the matrix manager may be directed to calculate disk locations as specified in the buffer and then placed in the xy field matrix. Single disks require no calculations for matrix placement. Disks which are part of line segments composed of N disks require disk location calculations. This calculation consists of determining N equidistant points on a directed line segment as specified in the buffer. Since this requires

simple algebra and trigonometry, this procedure will not be derived here. The equations used to find the x and y coordinates of the N disks are:

$$X(n) = X(n-1) + \sqrt{2}n\cos(a)$$

$$Y(n) = Y(n-1) + \sqrt{2}n\sin(a)$$

where

X(n) = x coordinate

Y(n) = y coordinate

X(n-1) = x coordinate of disk to the left

Y(n-1) = y coordinate of disk to the left

n = number of disk counting from the left

a = angle of directed line segment measured from the positive x axis in the counterclockwise direction.

Understanding of this equation and the significance of the $\sqrt{2}$ factor will become clearer after the next section.

The TFG Model and Computer Implementation

The TFG model is a two dimensional mathematical representation of a film segment. To understand the model and how the computer implements it, three aspects of the model are discussed here. They are field and disk mechanics, disk dynamics, and field wrap around.

Field and Disk Mechanics. The TFG model assumes a two dimensional field with an x axis length of XAXIS and a y axis length of YAXIS. In the computer, this field is composed of three subfields; the x field, y field, and an occupancy field. These subfields are used by the computer to store x, y, and occupancy data for each point in the model xy plane. Each subfield is represented by a matrix made of (XAXIS) x (YAXIS) unit cells. This is shown in Figure 3.4.

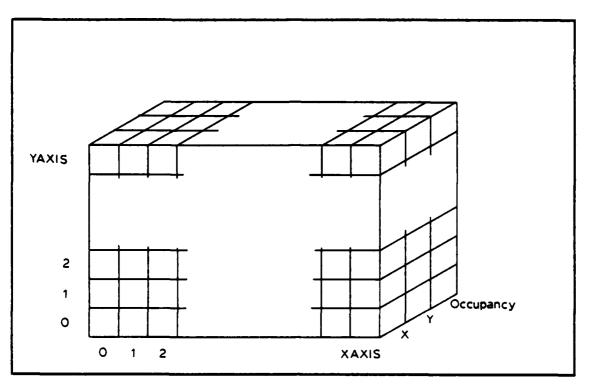


Fig. 3.4. Computer Subfields

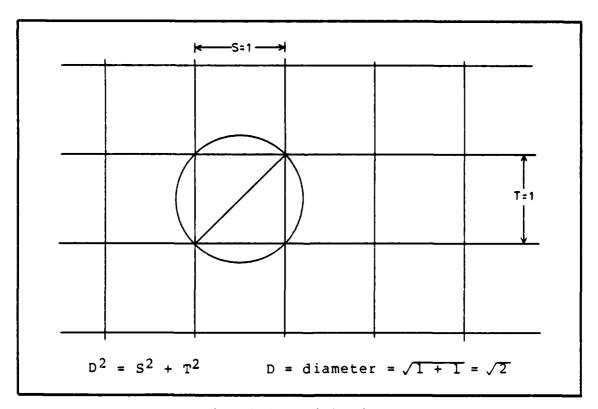


Fig. 3.5. Disk Size

Particles within the xy plane are represented in the model by hard disks. All disks are of the same diameter and the diameter is such that only one disk can fit in a unit cell, i.e. the disk diameter is equal to the diagonal of a square unit cell. In other words, a disk diameter is equal to the $\sqrt{2}$ (See Figure 3.5). Disks are therefore represented in the computer by a disk radius and center coordinates. computer stores disk coordinates in the matrix (See Figure 3.4) by storing each coordinate in the unit cell of the corresponding field. Unit cell addresses are made by truncating the coordinates. For example, consider a disk at location (4.3721, 25.9125). After truncation, this would become (4,25). The matrix cell assigned to the x and y coordinates respectively would be cell (4,25,1) and (4,25,2). 4.3721 would be stored in cell (4,25,1), 25.9125 would be stored in cell (4,25,2), and a 1 would be stored in cell (4,25,3) to indicate valid data in (4,25,1) and (4,25,2). The occupancy field can only contain a 0 or 1. A 0 indicates that the cell is unoccupied and any data contained by that cell in the x or y field is to be ignored. A l, on the other hand, indicates that the cell is occupied and the corresponding x and y field cells contain good data.

Disk contact, as shown in Figure 3.6, is accomplished by placing the disk center one radius from a surface. It is not accomplished by checking for an intersection of the disk surface with some other surface. Likewise, two disks come into contact when their centers are the $\sqrt{2}$ or one diameter

apart. Finally, a third disk may not pass between two other disks unless the centers of the two other disks are separated by more than two disk diameters.

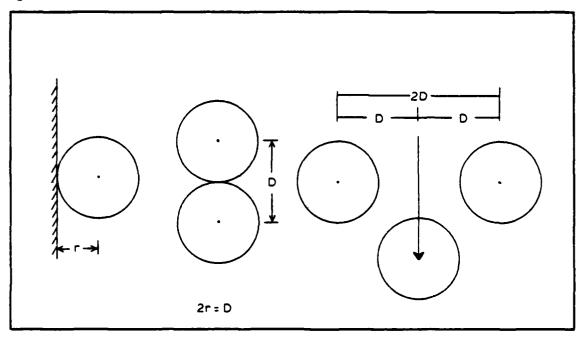


Fig. 3.6. Disk Contact

<u>Disk Dynamics</u>. In the TFG model, incident hard disks travel within the field on a straight line which is inclined at an angle A from the y axis. The values of the x coordinate at which this line intersects the x axis are chosen randomly. Each hard disk travels on the straight line until it comes in contact with one of the already deposited hard disks. Furthermore, the incident disk always remains in contact with the disk in the film with which it first made contact (base disk). After collision the incident disk relaxes or moves along the base disk perimeter until it reaches the nearest "pocket" where it makes contact with a disk which has been previously deposited (See Figure 3.7).

The disk dynamics described here and pictured in Figure 3.7 are implemented in the computer through two algorithms. The first is the collision point determination algorithm. It tracks the particle in and calculates where the incident disk center is located upon collision. The second is the roll and rest point determination algorithm. Its function is to locate the nearest rest point and calculate where the incident disk center will be when it comes to rest.

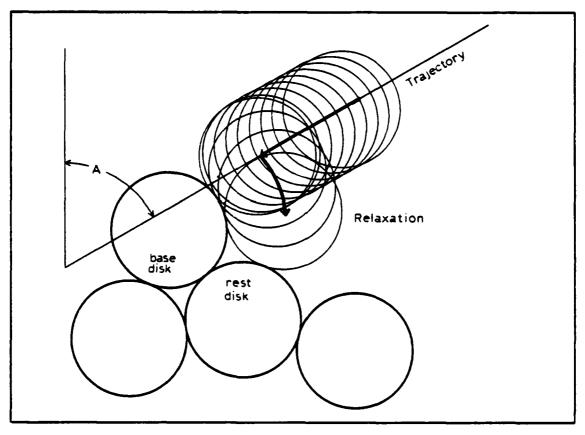


Fig. 3.7. Disk Contact and Relaxation

Collision Point Determination. There are many ways of implementing the tracking of a particle through its trajectory and simultaneously scanning the surrounding area for possible collision partners. The most obvious way would be

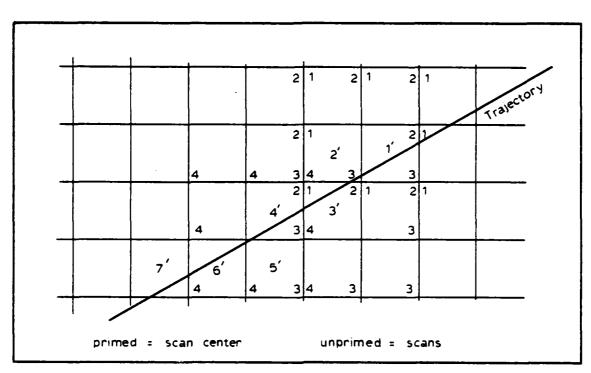


Fig. 3.8. Ordinary Area Scan

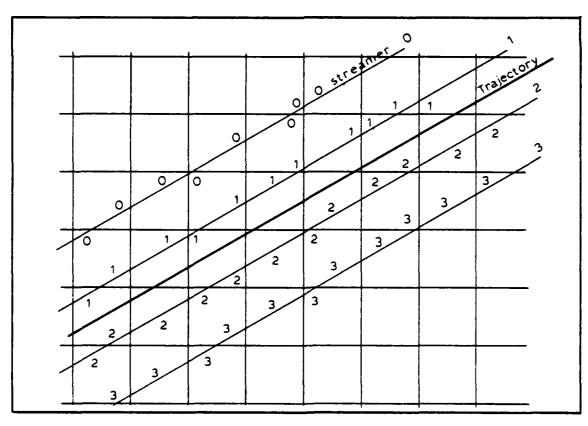


Fig. 3.9. TFG Model Scan

to start at the top of the field, move down the trajectory a step, scan for any particle within collision distance, move down another step, scan again and so-on (See Figure 3.8). This method, although easy to understand, is very inefficient. The program used and presented in Appendix A eliminates a lot of this methods inefficiencies.

The TFG program used reduces the inefficiency by two separate variations in the implementation of the model. First, the program stores and constantly maintains what the highest y cell value is. Trajectory tracking and collision scanning start one unit cell above this y value and therefore eliminate needless tracking and scanning for base cells. Second, the scanning technique used to find base cells is not an area search after each step as shown in Figure 3.8. This method would check the occupancy of a number of given cells many times. Instead, as shown in Figure 3.9, four streamers parallel to the trajectory search a "collision corridor" for occupancy in any cell that they contact. The streamers scan continues until encountering an occupied cell not previously encountered by another streamer. Concurrent with streamer scanning, occupied cells encountered are compared to see which would be the collision partner or base disk. Base disk determination is accomplished by trying all candidate base disks to see which yields the largest incident disk y coordinate.

Three items need to be expanded upon before moving on. The first is the term "collision corridor". From the

discussion on disk mechanics, it is known that a disk must be one disk diameter away from another disk for them to be in contact. Therefore, in order for a disk to be a collision partner with the incident disk, the disk must be within one diameter from the incident disk trajectory line. The area swept out by the perpendicular one diameter distance on both sides of the trajectory line is the collision corridor.

Next is the streamer spacing. Perpendicular spacing between streamers is always constant and equal. The spacing is chosen so that no matter what angle the streamers are at, no unit cell can be placed between them. At the same time the number of streamers should be as small as possible so that efficiency is kept high. Since the collision corridor is 2D thick or $2\sqrt{2}$ (see Figure 3.6), four streamers are required to ensure coverage. Their perpendicular spacing is $2\sqrt{2}/3$. The x axis intercepts of these streamers can be determined from,

$$S = a + \frac{2\sqrt{2}n}{3\cos(A)}$$

where

a = x coordinate of the left most streamer

A = deposition angle measured from substrate normal

n = streamer number starting with 0 and counting to the left (see Figure 3.9)

and

 $\frac{1}{\cos(A)}$ = x axis correction for A other than zero.

Finally, the incident disk center coordinates are found by calculating the intersection of the trajectory line

equation and the one diameter contact circle. This is shown in Figure 3.10 and the equations for the coordinates are:

$$Y = \frac{-\left(\frac{(a-h)}{m} - k\right) + \sqrt{r^2\left(\frac{1}{m^2} + 1\right) - \left((a-h) + \frac{k}{m}\right)^2}}{\left(\frac{1}{m^2} + 1\right)}$$

$$X = tan(A)Y + a$$

where

a = x intercept of trajectory line

h = x coordinate of the circle center

k = y coordinate of the circle center

A = deposition angle from substrate normal

m = tangent of A

r = disk radius

The derivation (See Appendix B) of these equations consists of simple algebra and trigonometry.

Roll and Rest Point Determination. Once the base disk is determined, the incident disk will roll around the base disk perimeter until it makes contact with a third disk. This third disk or rest disk is determined by finding that disk which allows the incident disk to move the shortest distance (See Figure 3.7). Then the final location of the incident disk is recorded in the field.

The program implements this by searching a seven by seven unit cell area around the base disk unit cell. All occupied cells which contain disk center coordinates within a two disk diameter radius of the base disk center are considered as possible rest disks. Then all of the rest position coordinates given the possible rest disks are found. The distances from the collision point to all possible rest

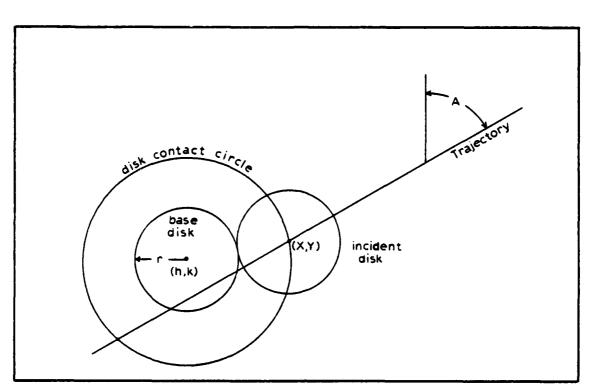


Fig. 3.10. Collision Point Determination

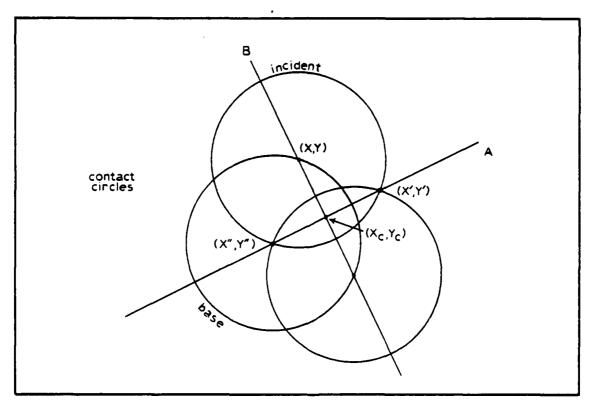


Fig. 3.11. Roll and Rest Point Determination

points are calculated and the shortest selected. Those rest point coordinates are then stored in the field matrix.

The formulas for finding the rest points are actually quite simple. They are:

$$X = \frac{X'R \pm \sqrt{X'^2R^2 - R(R^2 - 8Y'^2)}}{2R}$$

$$Y = \frac{Y'R \pm \sqrt{Y'^2R^2 - R(R^2 - 8X'^2)}}{2R}$$

where

$$R = (X'^2 + Y'^2)$$

and

X' = x separation of base and rest disk centers
Y' = y separation of base and rest disk centers.

The derivation of these formulas (See Appendix B) is based on the fact that the coordinates of the final resting position must be a distance of one disk diameter from the base and rest disk centers. This means that the coordinates of final resting position must be the center of a circle which passes through the base and rest disk centers. This is shown in Figure 3.11.

Field Wrap Around. In the TFG model, a field wrap around is provided. This makes the field periodic. So when film growth extends beyond the right boundary it is shifted back into the field on the left side. This makes more efficient use of the computer memory available and provides a means of recapturing data lost when it extends beyond the right boundary.

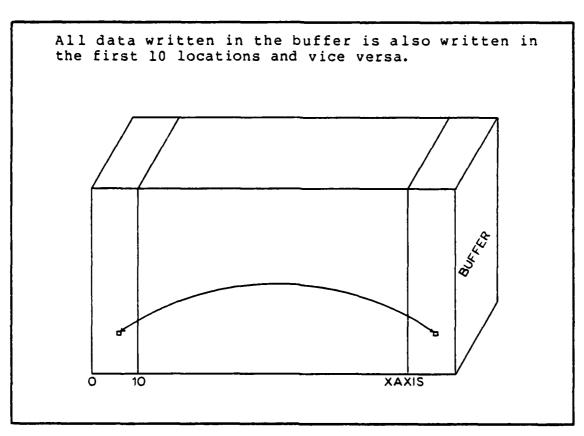


Fig. 3.12. Field Wrap Around Buffer

The implementation of the wrap around feature was accomplished by providing a ten unit buffer extended off the right side of the field (See Figure 3.12). This buffer is used simply to keep the collision point determination and roll and rest point determination algorithms simple. The buffer serves no other functional purpose. If the buffer were not provided, additional algorithms would have to be added to maintain synchronization between cells on the right side of the field and cells on the left. For example, in the roll and rest point determination algorithm, a seven by seven unit cell area around the base disk is searched for possible rest disks. If the base disk is centered on a y axis unit cell,

and no buffer is provided, part of the search pattern would be shifted to the left side of the field. However those cells on the left side of the field could not produce any possible rest disks, since they would be outside the two disk diameter radius. Consequently, film growth would be stopped at the right boundary. The only correction to this can be provided by a shifting correction algorithm within the rest point determination algorithm or a simple buffer.

TFG Analyzer

The TFG Analyzer provides the TFG simulator a means of determining the density, relative density, and the angle of columnar growth. It consists of two subprograms. One of the subprograms calculates field densities where the other calculates angle correlation numbers to be used in angle analysis.

Density. The theory of operation for density analysis is straight forward. Analysis of the density is not performed on the exact x and y coordinates but on the occupancy held matrix data. The density is found by

DEN = DSKCNT/CELCNT

where

In addition to standard density, a relative density is also determined (see Appendix B). This is a density relative to hexagonal packing in two dimensions and is given by

RDEN = $\sqrt{3}$ DEN.

Angle. The theory of operation for angle correlation is a little more involved and builds off the density theories. In this subprogram, a correlation number is determined for all whole degree angles from 0 to 89. The angle with the largest correlation number is the angle of columnar growth.

The correlation number for a given angle is found in several steps. First, the relative density of a two column trajectory is calculated. Then a modified average deviation from the relative film density is found. If the line density is less than or equal to the relative density, the average deviation is calculated by:

$$S = [(RDEN - DENLIN)/(RDEN)]^2$$

otherwise

$$S = [(DENLIN - RDEN)/(1 - RDEN)]^2$$

where

RDEN = the relative density of the film DENLIN = the relative density of the trajectory.

The trajectory is then slid over one unit cell and the average deviation is found again. This process is repeated until the whole x axis has been traversed. All of the average deviations are then averaged together and this becomes the correlation number.

IV Validation of the Computer Program

Validation of computer programming is essential if any amount of confidence in a program are to be gained. It is for this reason that the program was checked with great detail to ensure that the programming was doing what was intended. Validation of the computer program/model consisted of four separate tests. These are explained below and are presented in the order in which they were accomplished.

Test one was a simple verification that the interactive logic and input was functioning properly. It consisted of trying all possible commands listed in the programs various menus and entering selected data where required. For example, one sequence tried was entering data in the substrate data buffer by entering A, 1, .2, 1.5, 225, 0. This sequence should create two lines in the data buffer as follows:

NDSK 1	X Coord	Y Coord	Angle
	.2000	1.5000	.0000
225	.0000	.0000	.0000

Test two was designed to verify the substrate data entry and substrate construction. It consisted of three separate scenarios which generated flat, triangular well, and square well shaped substrates. Each scenario produced a printout giving cell content after substrate construction. The cell content was then compared to hand calculated results. Printout coding used in this test are indicated in the Fortran listing in Appendix A by a CT2 in the left most columns.

Test three was designed to verify the particle trajectory, collision point determination, roll and rest point determination, wrap around, and matrix full routines. test consisted of two phases. The first, used a special version of the TFG simulator which was modified to print out all its calculations in the above routines and its random number generator was primed to give 10 known numbers. These numbers produced incoming particles which tested the limits of many critical routines. The printouts of these 10 situations were then compared to calculated particle movement and rest points. The second phase also used a special version of the TFG simulator. This version was modified to check for cell overwriting and spacing between the incoming particle, the collision particle, and the rest particle. To ensure that even the most minute error in the model would be caught, 340,000 particles were deposited (20,000 disks at 17 random deposition angles every 5 degrees from 0 to 80 degrees). Again, applicable printout coding is indicated in Appendix A.

Test four was designed to verify proper operation of the analysis routines. Again, a special version of the TFG simulator was used. Here the simulator was modified to print out various steps in the analysis. These are indicated in Appendix A by CT4. In addition, a test case was then run and compared with expected results.

After some programming error correction, all items tested passed with no errors noted. It should also be noted that with testing and normal program operation no errors to

date have been found. This adds up to over .5 million disks deposited.

V TFG Simulator Results

Once a TFG simulator was made and tested, the next important step was to run various depositions and check the results with those of known experimental works. Therefore, analysis of nine depositions were made. They were at A equals 0, 10, 20, 30, 40, 50, 60, 70, and 80 degrees. With this selection of deposition angles; density dependence on A, microstructure, and angle of columnar growth can be compared with experimental results and observations presented in Chapter II.

It should also be noted that the analysis was made of data in a 320x240 matrix on rows between 20 and 170. The 150 unit cell analysis was done to eliminate density variations which have been observed at the bottom and top of the film.

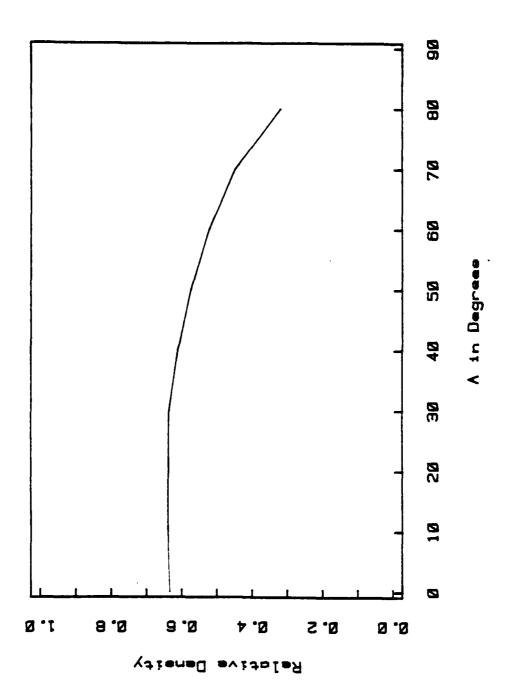
Density. The relative density of the previously stated depositions are shown in Figure 5.1. Except for the 0 and 10 degree depositions, larger deposition angles produce lower density material. This small disagreement could easily be caused by density variations in rows near the upper and lower analysis bounds. Density has been observed in other deposition to vary slightly.

Microstructure. The microstructure plots in Figures 5.2-5.5 are high density plots with 15 to 25 thousand disks. Only four of the nine depositions are shown here, since the structures do not change dramatically over 10 degree

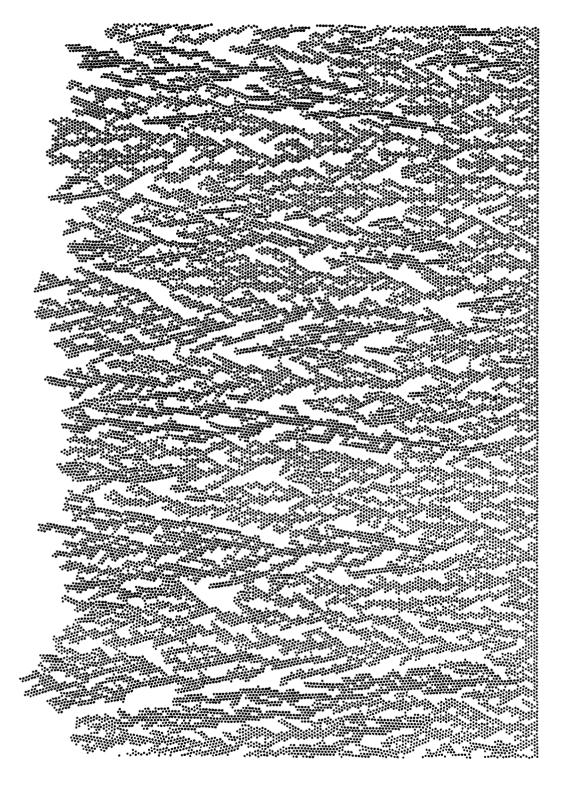
intervals. The plots shown are of 0, 30, 60, and 80 degree depositions.

Column Angle. Angle analysis plots of all depositions are presented in Figures 5.6-5.14. These are presented here in their entirety because the angles, as determined by the maximum correlation points, are not always conclusive. Some have secondary maximum points which could be the angle of columnar growth. In Figure 5.15, all the maximum and secondary maximum points are plotted on a graph with a plot of the tangent rule. The results are relatively close and again the variation could be caused by density variations. Only this time the density variations would have to be in the local area of the trajected line.

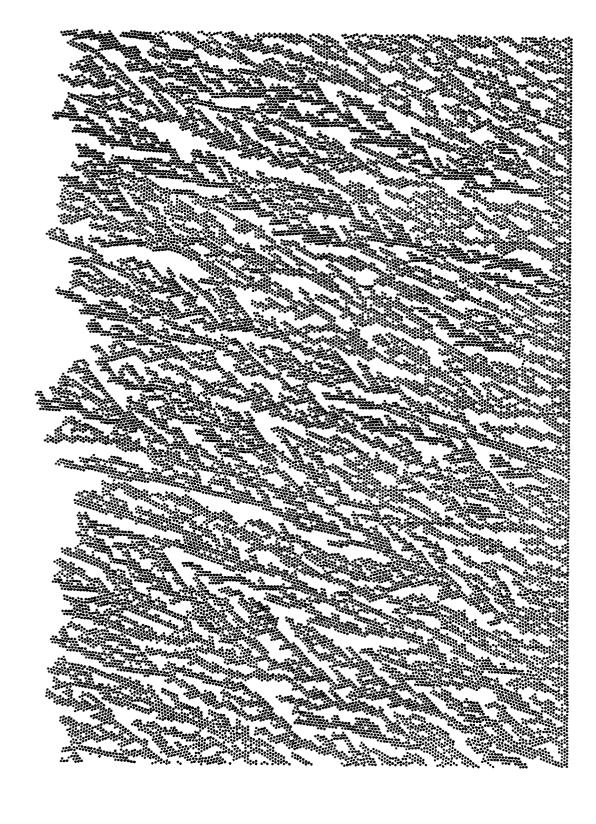
DENSITY COMPARISON



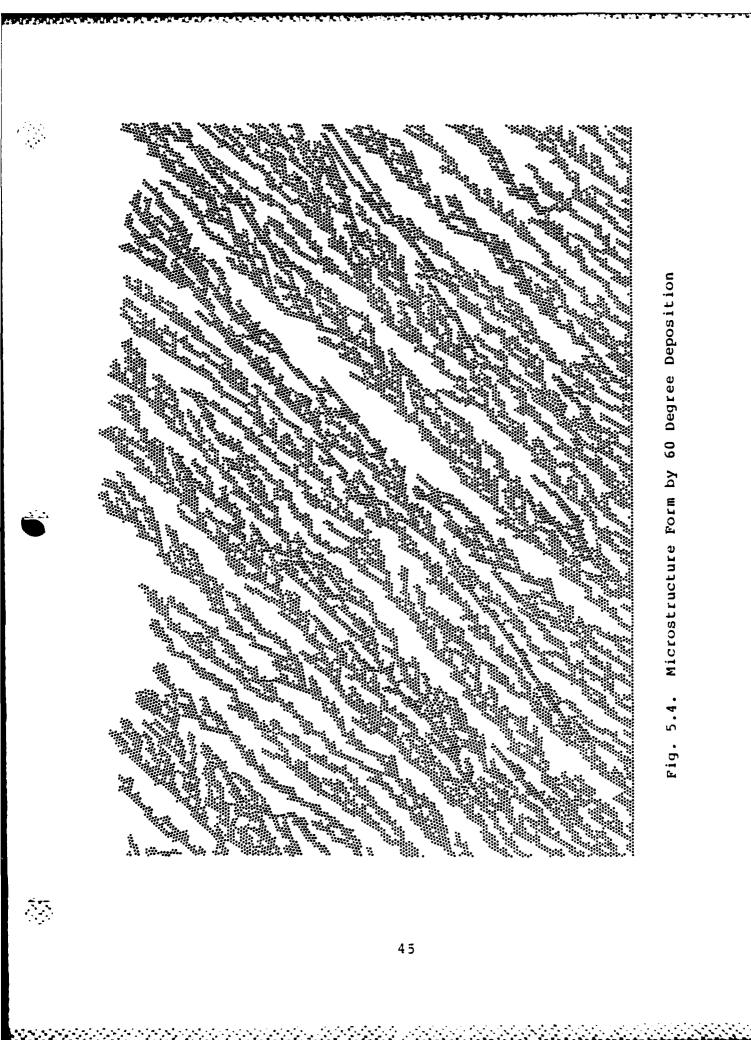
Relative Density at Deposition Angles Less Than 80 Degrees Fig. 5.1.



Normal Incidence ζ Form Microstructure



ig. 5.3. Microstructure Form by 30 Degree Deposition



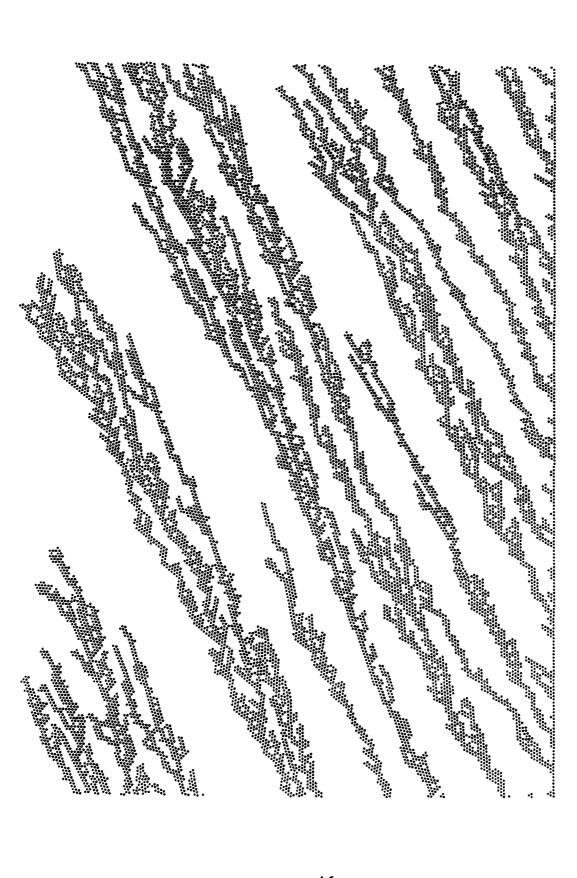
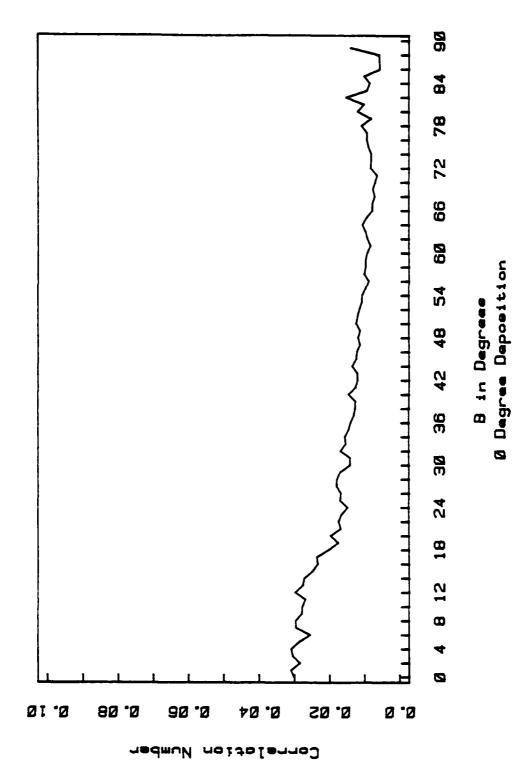
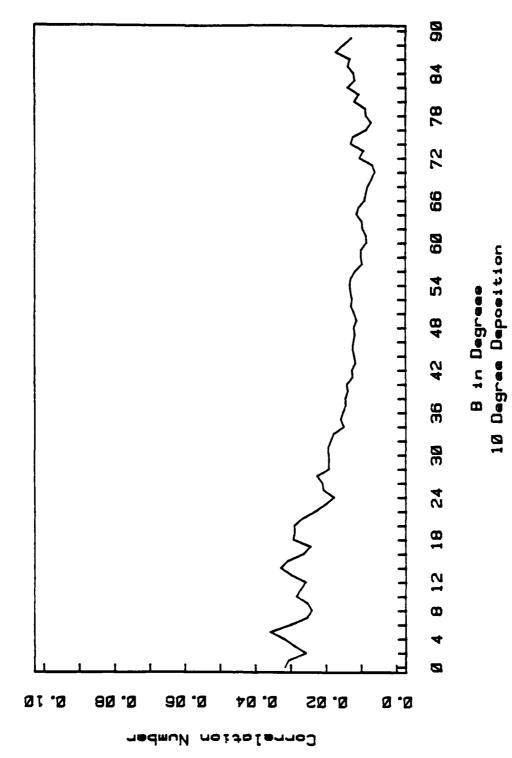


Fig. 5.5. Microstructure Form by 80 Degree Deposition

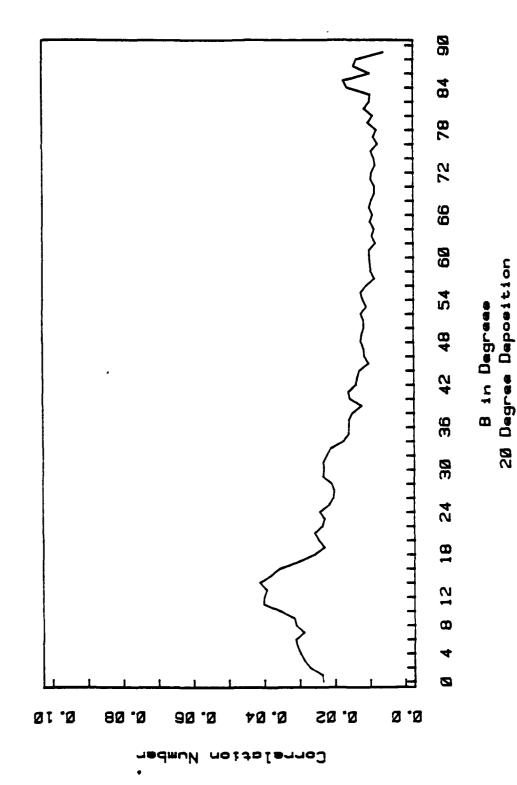


Columnar Angle Analysis of Film Formed by Normal Incidence Deposition Fig. 5.6.

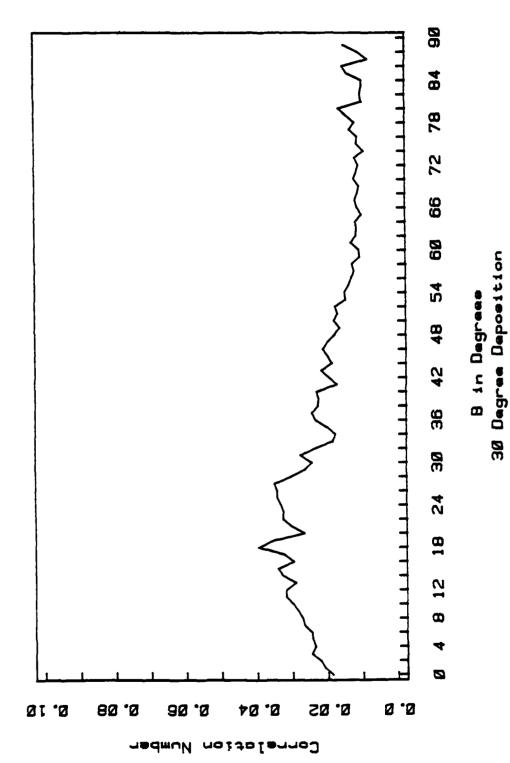
A RECOGNICATION DESCRIPTION



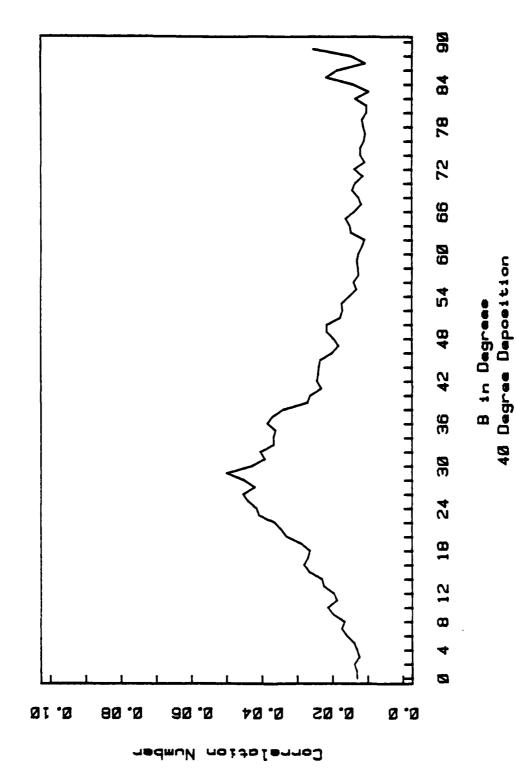
Columnar Angle Analysis of Film Formed by 10 Degree Deposition Fig. 5.7.



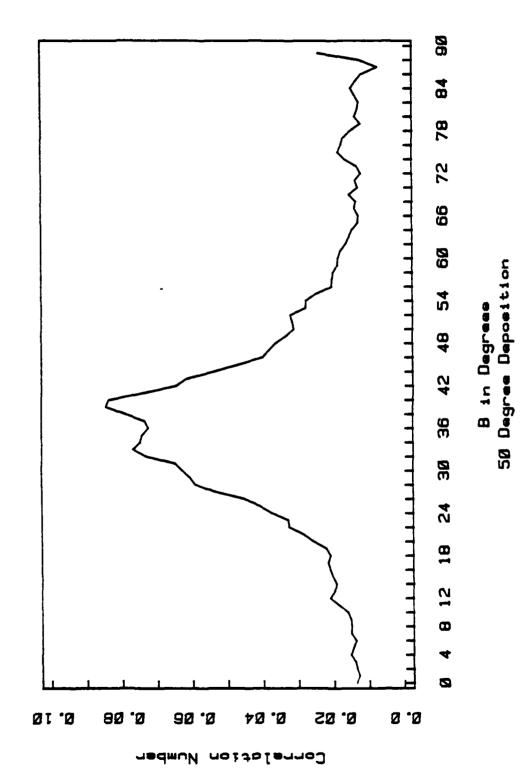
Columnar Angle Analysis of Film Formed by 20 Degree Deposition Fig. 5.8.



Columnar Angle Analysis of Film Formed by 30 Degree Deposition

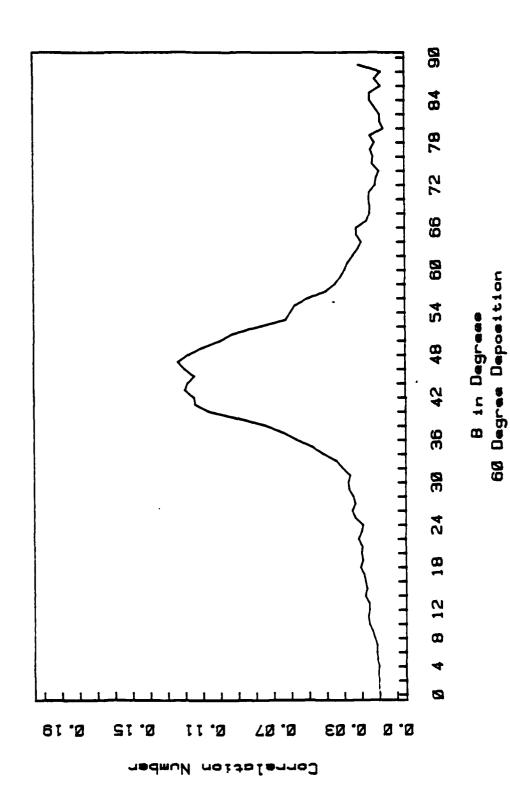


Columnar Angle Analysis of Film Formed by 40 Degree Deposition Fig. 5.10.

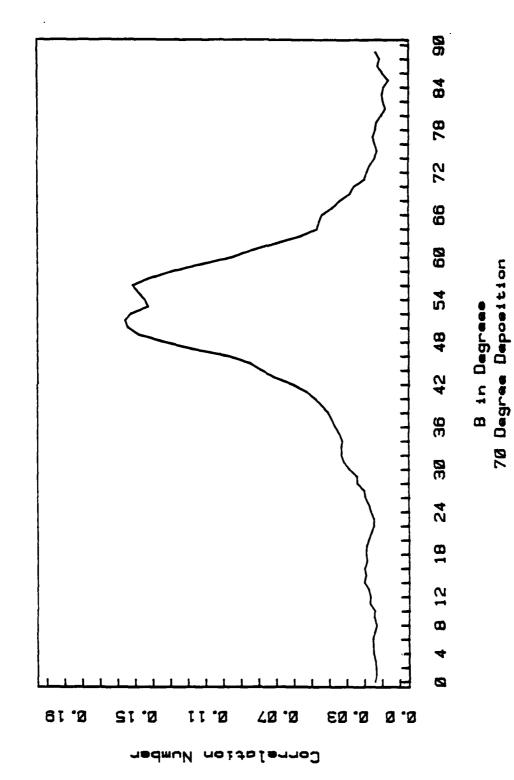


Columnar Angle Analysis of Film Formed by 50 Degree Deposition Fig. 5.11.

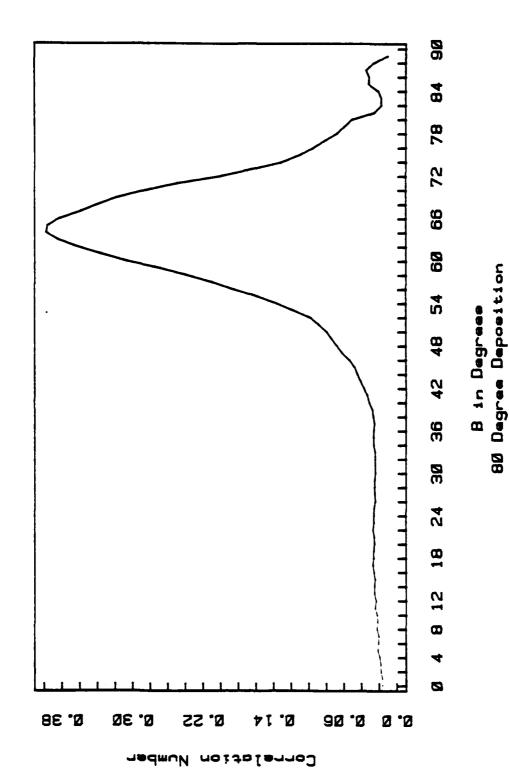
The state of the last



Columnar Angle Analysis of Film Formed by 60 Degree Deposition

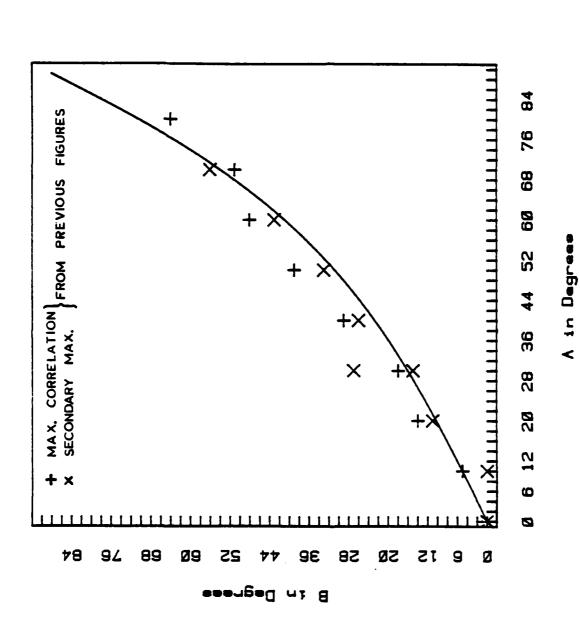


Columnar Angle Analysis of Film Formed by 70 Degree Deposition



Columnar Angle Analysis of Film Formed by 80 Degree Deposition





Comparison of Column Angle Determined, With Tangent Rule Predictions Fig. 5.15.

VI Conclusions and Recommendations

From the results in chapter V and the experimental results outlined in chapter II, it is evident that this simple, limited-mobility deposition scheme yields films that reproduce the general features observed experimentally. These features are:

- Film density decreases with increasing A.
- 2. Column-like higher density regions appear at angle B < A. Column orientation agrees reasonably well with the tangent rule.
- 3. Column separation and definition increases with increasing A.

In view of the assumption made and the results obtained two logical follow on efforts could improve the computer model. First, expanding this two-dimensional model to three would reverify the results here and would also provide a means of verifying the change in columnar shape with deposition angle. Second, and most importantly, particle energy was treated in a crude manner to say the least. Consequently, the mobility of the model does not accurately portray mobilities found in real life. Since mobility and density are directly proportional, a study of a variety of model mobilities might yield some good insight into how mobility could be addressed in this model so as to obtain realistic film densities. If either or both of these model expansions take place a more accurate result should be ob-

tained. However, memory capacity plays an extremely large role in such an undertaking. The internal memory capacity required needs to be kept in a finite bound. One way of helping this situation is to reduce the size of the xy plane. Another would be to develop an algorithm which allows the internal memory to keep track of only the upper portion of the thin film. As the lower portions become buried and inactive, the data can be transferred to disk storage, thereby conserving internal memory.

As for the accuracy of the results, two comments are offered. First, density calculation for angle analysis need to be changed to allow for local density variations. Second, a great amount of weight should not be put on these column angle determinations alone. If many depositions were run for each deposition angle a more reliable determination of column angle and relative density could be obtained.

Still, the following observation can be made. Since the results reproduce the general characteristics of thin film growth, and neither momentum, oxygen absorption, crystalline texture, nor facet formation figure in the simulation process; low mobility and geometric shadowing seem to be the main driver in the development of the microstructure.

APPENDIX A

Fortran Listing of TFG Simulator

```
0000000
                         "Thin Film Growth Simulator"
                                 Version 1.00
                        Written by Jeffrey A. Stefoneck
                                   1 Oct 84
        This program simulates vapor deposited thin film growth.
C
        It was designed to run on the VAX with an HP 7220 plotter and
requires Fortran 77, IMSL, and S.
                       MAIN PROGRAM START-UP
                         AND INTERFACE LOOP
                 ******* ARRAY DEFINITION *******
С
C
00010
        DOUBLE PRECISION DSEED
        REAL RN, ANG, CELCNT, SIZE
        INTEGER XAXIS, YAXIS, ZAXIS, TNDSKS
        DIMENSION DBUFF(3,240), NDSK(240)
        DIMENSION CELL(0:329,0:239,3)
CT2,3
        DIMENSION PBUFFX(6), PBUFFY(6)
        DIMENSION WBUFF(100,3)
        REAL DIRIND(0:89)
        CHARACTER*2 CANS
        XAXIS=319
        YAXIS=239
        ZAXIS=3
        SIZE=0
CCCC
                    ***** SIGN ON ******
C
00020
        WRITE(6,09001)
```

```
C
C
                 ******** ARRAY INITIALIZATION ***
C
        CALL INITB (DBUFF, NDSK)
        CALL INITM (CELL, TNDSKS, IHY)
        DSEED=1831728294.D0
C
C
c
                ******* INTERFACE LOOP *******
C
01000
        WRITE(6,09010)
        READ (5,09012) DATE
        DSEED=DSEED-DATE
01001
        WRITE(6,09011)
01002
        READ(5,09012) CANS
        IF (CANS.EQ.'B') THEN
                GO TO 20001
        ELSE IF (CANS.EQ.'D') THEN
                GO TO 30001
        ELSE IF (CANS.EQ.'M') THEN
                GO TO 40001
CT2,3
        ELSE IF (CANS.EQ.'P')
                               THEN
CT2,3
                GO TO 50001
        ELSE IF (CANS.EQ.'A') THEN
                GO TO 60001
        END IF
        WRITE(6,09013)
        GO TO 01002
C
C
C
                ******* START-UP AND INTERFACE MSGS ***
C
C
        FORMAT(10(2X/),25X,'Thin Film Growth(TFG) Simulator'/,34X,'Versi
09001
     Con 1.00'/,35X,'========'/,25X,'Written by Jeffrey A. Stefoneck'/
     C,36X,'1 Oct 84'/,9(2X/)
09010
        FORMAT('Enter date (MMDDYYYY).
                                         '$)
        FORMAT(7(2X/),27X, 'Thin Film Growth Simulator'/,2(2x/),15X, 'B-Bu
09011
     Cffer Editor'/,15x,'D-Deposit'/,15x,'M-Matrix Manager'/,15x,'A-Anal
     Cysis'/,
CT2,3
          Cl5X, 'P-Print Cell Content'/,
     Cllx,'Break-Exit to Unix'/,7(2X/))
09012
        FORMAT(A1)
09013
        FORMAT(15X,'Incorrect response, please try again.'/)
C
C
```

```
0000000000
                           BUFFER EDITOR
                 ******* BUFFER EDITOR INTERFACE LOOP **
C
C
20001
        WRITE(6,29001)
20002
        READ(5,29003) CANS
        IF (CANS.EQ.'S') THEN
                 GO TO 21000
        ELSE IF (CANS.EQ.'M') THEN
                 GO TO 22000
        ELSE IF (CANS.EQ.'A') THEN
                 GO TO 23000
        ELSE IF (CANS.EQ.'R') THEN
                 GO TO 24000
        ELSE IF (CANS.EQ.'D') THEN
                 GO TO 26000
        ELSE IF (CANS.EQ.'E') THEN
                 GO TO 01001
        ELSE IF (CANS.EQ.'ED') THEN
                 GO TO 30001
        ELSE IF (CANS.EQ.'EM') THEN
                 GO TO 40001
CT2,3
        ELSE IF (CANS.EQ. 'EP') THEN
CT2,3
                 GO TO 50001
        ELSE IF (CANS.EQ.'EA') THEN
                 GO TO 60001
         END IF
        WRITE(6,29002)
        GO TO 20002
C
C
C
                     ****** BUFFER EDITOR SHOW COMMAND ***:
C
C
21000
        DO 21003 L=1,20
                 WRITE(6,29010)
                 DO 21001 LL=1,15
                         K=15*(L-1)+LL
                         WRITE(6,29011) K, NDSK(K), (DBUFF(J,K), J=1,3)
                         IF(K.GE.240) GO TO 21002
                 CONTINUE
21001
21002
                 WRITE(6,29012)
                 READ(5,29003) CANS
                 IF(CANS.EQ.'E') GO TO 20001
                 IF(K.GE.240) GO TO 21004
```

```
21003
        CONTINUE
21004
        GO TO 20001
C
C
                ****** BUFFER EDITOR MODIFY COMMAND *******
C
C
22000
        WRITE(6,29020)
        READ *, LENTRY
22002
        IF ((LENTRY.GT.0).AND.(LENTRY.LE.240)) GO TO 22003
        IF (LENTRY.EQ.0) GO TO 20001
        WRITE(6,29002)
        GO TO 22002
22003
        WRITE(6,29022)
22004
        READ *, NDSK(LENTRY)
        S=XAXIS
        T=YAXIS
        HYP = SQRT(S**2+T**2)
        IF ((NDSK(LENTRY).GE.0).AND.(NDSK(LENTRY).LE.HYP)) GO TO 22005
        WRITE(6,29002)
        GO TO 22004
22005
        IF (NDSK(LENTRY).EQ.0) GO TO 20001
        IF (NDSK(LENTRY).GT.1) GO TO 22010
        DBUFF(3, LENTRY) = 0
        WRITE(6,29032)
22006
        READ *,DBUFF(1,LENTRY)
        IF ((DBUFF(1,LENTRY).GT.0).AND.(DBUFF(1,LENTRY).LE.XAXIS)) GO TO
     C22007
        WRITE(6,29002)
        GO TO 22006
22007
        WRITE(6,29034)
22008
        READ *,DBUFF(2,LENTRY)
        IF ((DBUFF(2,LENTRY).GT.0).AND.(DBUFF(2,LENTRY).LE.YAXIS)) GO TO
     C22009
        WRITE(6,29002)
        GO TO 22008
        IF (NDSK(LENTRY).EQ.1) GO TO 22012
22009
22010
        DBUFF(1, LENTRY) = 0
        DBUFF(2, LENTRY) = 0
        WRITE(6,29035)
        READ *,DBUFF(3,LENTRY)
22011
        IF ((DBUFF(3,LENTRY).GE.0).AND.(DBUFF(3,LENTRY).LT.360)) GO TO 2
     C2012
        WRITE(6,29002)
        GO TO 23011
22012
        GO TO 22000
C
C
C
                 ****** BUFFER EDITOR ADD COMMAND *******
C
         DO 23002 L=240,1,-1
23000
                 IF (NDSK(L).GT.0) GO TO 23003
```

```
23002
       CONTINUE
        LENTRY=LENTRY+1
23003
       WRITE(6,29030) LENTRY
23004
        READ *, NDSK (LENTRY)
        S=XAXIS
        T=YAXIS
        EMX=SQRT(S**2+T**2)
        IF ((NDSK(LENTRY).GE.0).AND.(NDSK(LENTRY).LE.EMX)) GO TO 23005
        WRITE(6,29002)
        GO TO 23004
23005
        IF (NDSK(LENTRY).EQ.0) GO TO 20001
        IF (NDSK(LENTRY).GT.1) GO TO 23010
        WRITE(6,29032)
23006
        READ *, DBUFF(1, LENTRY)
        IF ((DBUFF(1,LENTRY).GT.0).AND.(DBUFF(1,LENTRY).LE.XAXIS)) GO TO
     C23007
        WRITE(6,29002)
        GO TO 23006
23007
        WRITE(6,29034)
23008
        READ *,DBUFF(2,LENTRY)
        IF ((DBUFF(2,LENTRY).GT.0).AND.(DBUFF(2,LENTRY).LE.YAXIS)) GO TO
     C23009
        WRITE(6,29002)
        GO TO 23008
23009
        IF (NDSK(LENTRY).EQ.1) GO TO 23012
23010
        WRITE(6,29035)
23011
        READ *,DBUFF(3,LENTRY)
        IF ((DBUFF(3,LENTRY).GE.0).AND.(DBUFF(3,LENTRY).LT.360)) GO TO 2
     C3012
        WRITE(6,29002)
        GO TO 23011
23012
        LENTRY=LENTRY+1
        GO TO 23003
C
C
C
                ****** BUFFER EDITOR RESET COMMAND
C
24000
        CALL INITB (DBUFF, NDSK)
        GO TO 20001
C
C
C
                C
C
26000
        WRITE(6,29060)
26002
        READ *, IANS
        IF((IANS.GE.1).AND.(IANS.LE.240)) GO TO 26003
        IF(IANS.EQ.0) GO TO 20001
        WRITE(6,29061)
        GO TO 26002
        NDSK(IANS) = 0
26003
        DBUFF(1,IANS) = 0
```

```
C
C
                   ****** BUFFER EDITOR MSGS ****
C
C
29001
        FORMAT(6(2X/),25X,'DATA BUFFER EDITOR
                                                 ',2(2X/),15X,'S-Show Con
     Ctents of Data Buffer'/,15X,'M-Modify Contents of Data Buffer'/,15X
     C,'A-Add Data to End of Data Buffer String'/,15x,'D-Delete Data Buf
     Cfer Line'/,15X,'R-Reset Data Buffer to Zero'/,14X,'E?-Exit',6(2X/)
29002
        FORMAT(2X/,15X,'Incorrect response, please try agian.',2X)
29003
        FORMAT(A2,$)
29010
        FORMAT(2X/,27('*'),' CONTENTS OF DATA BUFFER ',28('*')//,13X,'En
     Ctry N N Disks
                         X-Coord
                                      Y-Coord
                                                     Angle'/)
29011
        FORMAT(15X, 13, 6X, 13, 6X, 3(F8.4, 5X))
29012
        FORMAT('To scroll up, push any key (except E) and CR.'/,'To exit
     C to main menu push E and CR.')
C
29020
        FORMAT('Modifying data',2X/,9X,'What line number? '$)
C29021
        FORMAT(17)
29022
        FORMAT(10x,'Number of disks? '$)
29030
        FORMAT('Adding data on line ',I3,'.'/,10X,'Number of disks
     C? '$)
C29031
        FORMAT(17)
        FORMAT(13X,'X Coordinate? '$)
29032
C29033
        FORMAT(F11.4)
29034
        FORMAT(13X,'Y Coordinate? '$)
29035
        FORMAT(20X, 'Angle? '$)
C29036
        FORMAT(F8.4)
29040
        FORMAT(13,2x,13,2x/,13,2x,15)
29041
        FORMAT(E15.9,2X,E15.9)
C
29060
        FORMAT(2X/,'What line do you wish deleted?
29061
        FORMAT(2X/,'No such line. Answer should be 1-240.')
C
C
```

DBUFF(2,IANS)=0 DBUFF(3,IANS)=0 GO TO 26000

C

C

```
000000
                           TFG DEPOSITOR
C
C
                 ****** TFG DEPOSITOR INTERFACE LOOP
C
C
30001
        WRITE(6,39000)
30002
        READ *, IANS
        IAREA=XAXIS*YAXIS*.6
        IF ((IANS.GE.0).AND.(IANS.LE.IAREA)) GO TO 30003
        IF (IANS.EQ.0) GO TO 20001
        WRITE(6,39002)
        GO TO 30002
30003
        WRITE(6,39003)
30004
        READ *, ANS
        IF ((ANS.GE.0).AND.(ANS.LE.80)) GO TO 30005
        WRITE(6,39005)
        GO TO 30004
30005
        WRITE (6,39006) ANS, IANS
30006
        READ(5,39007) CANS
        IF (CANS.EQ.'E') THEN
                 GO TO 1001
        ELSE IF (CANS.EQ.'EB') THEN
                 GO TO 20001
        ELSE IF (CANS.EQ.'EM') THEN
                 GO TO 40001
CT2,3
        ELSE IF (CANS.EQ.'EP') THEN
CT2,3
                 GO TO 50001
        ELSE IF (CANS.EQ.'EA') THEN
                 GO TO 60001
        ELSE IF (CANS.EQ.'R') THEN
                 GO TO 30001
        ELSE IF (CANS.EQ.'D') THEN
                 GO TO 31001
        END IF
        WRITE(6,39008)
        GO TO 30006
C
C
                 ******* TFG DEPOSITOR LOOP *****
cc
31001
        ANGLE= ANS
        NODSK=IANS
        RANGLE=ANGLE/57.29577951
        CA=COS (RANGLE)
```

D=TAN(RANGLE)

```
E=D*D+1
        C=0
        ND = 0
        NDDEP=0
        DO 31002 NTDEP=NODSK,1,-1
CT3
            print *,'NODSK=',NODSK
            IF (IHY.EO.(YAXIS-1)) GO TO 31004
C
č
C
                   --- RANDOM NUMBER GENERATION ----
C
C
31100
            RN=GGUBFS (DSEED)
            RAND=RN*(XAXIS+1)-1
CT3
            print *, 'RAND=', RAND
C
C
Č
                   --- COLLISION POINT DETERMINATION -----
C
            Y2=0
            DO 31205 ISTEP=0,3
CT3
                 print *,'ISTEP=',ISTEP
                 AA=RAND+1.414592654/CA
                 AS=RAND+.9428090416*(ISTEP/CA)
                 X=D*IHY+AS
                 JUMP=0
                 LX = X
                 DO 31204 IYS=IHY,0,-1
                     print *,'IHY=',IHY,' IYS=',IYS
CT3
                     X=D*IYS+AS
                     ISHFT=(INT(X/(XAXIS+1)))*(XAXIS+1)
                     NXS=INT(X-ISHFT)
                     LXS=INT(LX-ISHFT)
                     DO 31202 IXS=LXS,0,-1
CT3
                         print *,'LXS=',LXS,'IXS=',IXS,'NXS=',NXS
                         IF (CELL(IXS, IYS, 3).EQ.1) THEN
                              IF ((IXS.EQ.IXT).AND.(IYS.EQ.IYT)) GO TO 312
     C07
                              XMIN=D*CELL(IXS,IYS,2)+RAND-ISHFT
                              XMAX=XMIN+2.828427125/CA
                              print *,'Possible Cl (',CELL(IXS,IYS,1),',',
CT3
                               XMIN=',XMIN,'
CT3
         CCELL(IXS, IYS, 2),')
                                              XAMX, '=XAMX
                              IF (ISTEP.LT.2) THEN
                                  IF ((CELL(IXS,IYS,1).LT.XMIN).OR.(CELL(I
     CXS, IYS, 1) .GT.XMAX)) GO TO 31207
                                  A=AA-ISHFT
                                  F=CELL(IXS,IYS,2)-D*(A-CELL(IXS,IYS,1))
                                  G=(A-CELL(IXS,IYS,1))+D*CELL(IXS,IYS,2)
                                  Y=(F+SQRT(2*E-G*G))/E
                                  print *,'Y coord ',Y
CT3
                                  IXT=IXS
                                  IYT=IYS
```

```
IF (Y2.LT.Y) THEN
                                      Y2=Y
                                      IX1=IXS
                                      IY1=IYS
                                      A2=A
                                  END IF
                                  JUMP=1
                             ELSE
                                  IF ((CELL(IXS,IYS,1).LT.XMIN).OR.(CELL(I
     CXS, IYS, 1) .GT.XMAX)) GO TO 31207
                                  A=AA-ISHFT
                                  F=CELL(IXS,IYS,2)-D*(A-CELL(IXS,IYS,1))
                                  G=(A-CELL(IXS, IYS, 1))+D*CELL(IXS, IYS, 2)
                                  Y=(F+SQRT(2*E-G*G))/E
CT3
                                  print *,'Y Coord ',Y
                                  IXT=IXS
                                  IYT=IYS
                                  IF (Y2.LT.Y) THEN
                                      Y2=Y
                                      IX1=IXS
                                      IY1=IYS
                                      A2=A
                                  END IF
                                  JUMP=1
                              END IF
                         END IF
31207
                         IF (IXS.EQ.NXS) GO TO 31206
31202
                     CONTINUE
31206
                     LX = X
                     IF (JUMP.EQ.1) GO TO 31205
31204
                 CONTINUE
            CONTINUE
31205
             X2 = D \times Y2 + A2
             IF (IX1.LT.3) THEN
                 X2=X2+XAXIS+1
                 IX1=IX1+XAXIS+1
CT3
             print *,'Cl (',IX1,',',IY1,') Y2 ',Y2
C
C
C
                     -- REST POINT DETERMINATION ----
C
C
31300
             SHORT=18
             DO 31302 J=-3,3
                 IX3=J+IX1
                 DO 31301 K=-3,3
                     IY3=K+IY1
                     IF ((IY3.LT.0).OR.(IYS.GT.IHY)) GO TO 31301
                     IF (CELL(IX3,IY3,3).EQ.1) THEN
                          print *,'Possible Rest Cell (',IX3,',',IY3,')'
CT3
                          X31=CELL(IX3,IY3,1)-CELL(IX1,IY1,1)
```

```
Y31=CELL(IX3,IY3,2)-CELL(IX1,IY1,2)
                         R13SQR = (X31**2) + (Y31**2)
                         print *,'R13SQR=',R13SQR
CT3
                         IF ((R13SQR.GE.1.8).AND.(R13SQR.LE.8.0)) THEN
                              R=R13SOR
                              STX=(X31**2)*(R*R)-R*((R*R)-8*(Y31**2))
                              IF (STX.LT.0) THEN
                                  TX = 0
                              ELSE
                                  TX=SORT(STX)
                              END IF
                              STY=(Y31**2)*(R*R)-R*((R*R)-8*(X31**2))
                              IF (STY.LT.0) THEN
                                  TY = 0
                              ELSE
                                  TY=SQRT(STY)
                              END IF
                              DO 31303 L=-1,1,2
                                  IF (X31.GE.O) THEN
                                       X2T = (X31*R+L*TX)/(2*R)
                                  ELSE
                                       X2T = (X31*R-L*TX)/(2*R)
                                  END IF
                                  IF (Y31.LE.O) THEN
                                       Y2T = (Y31*R+L*TY)/(2*R)
                                  ELSE
                                       Y2T = (Y31*R-L*TY)/(2*R)
                                  END IF
                                  X22=X2T+CELL(IX1,IY1,1)-X2
                                  Y22=Y2T+CELL(IX1,IY1,2)-Y2
                                  R22SQR = (X22**2) + (Y22**2)
                                  print *,'R22SQR=',R22SQR
CT3
                                  IF (R22SQR.LT.SHORT) THEN
                                       SHORT=R22SQR
                                       X2F=X2T
                                       Y2F=Y2T
                                       IX3F=IX3
                                       IY3F=IY3
                                       FX31=X31
                                       FY31=Y31
                                       FR13SQ=R13SQR
                                   END IF
                              CONTINUE
31303
                          END IF
                      END IF
                 CONTINUE
31301
             CONTINUE
31302
             R13=SQRT(FR13SQ)
             print *,'R13=',R13
CT3
             X21=X2F
             Y21=Y2F
             R12SQR=X21**2+Y21**2
             X2=X2F+CELL(IX1,IY1,1)
```

```
Y2=Y2F+CELL(IX1,IY1,2)
            IX2 = INT(X2)
            IY2=INT(Y2)
CT3
            X23=X2-CELL(IX3F,IY3F,1)
CT3
            Y23=Y2-CELL(IX3F,IY3F,2)
CT3
             R23SQR=X23**2+Y23**2
CT3
             IF (((R12SQR.LE.1.8).OR.(R12SQR.GE.2.2)).OR.((R23SQR.LE.1.8)
CT3
        C.OR. (R23SQR.GE.2.2))) THEN
CT3
                 print *,'Rest Point Error--R12SQR=',R12SQR,'R23SQR=',R23
CT3
        CSQR
CT3
                 GO TO 80000
CT3
             END IF
CT3
             IF (CELL(IX2,IY2,3).EQ.1) THEN
CT3
                 print *,'Overwrite on cell (',IX2,',',IY2,')'
                 GO TO 80000
CT3
             END IF
CT3
             IF (IX2.GT.XAXIS) THEN
                 X2M=X2-(XAXIS+1)
                 IX2M=IX2-(XAXIS+1)
                 CELL(IX2M,IY2,1) = X2M
                 CELL(IX2M,IY2,2) = Y2
                 CELL(IX2M,IY2,3)=1
             ELSE IF (IX2.LT.10) THEN
                 X2M=X2+(XAXIS+1)
                 IX2M=IX2+(XAXIS+1)
                 CELL(IX2M,IY2,1) = X2M
                 CELL(IX2M,IY2,2) = Y2
                 CELL(IX2M,IY2,3)=1
             END IF
             CELL(IX2,IY2,1) = X2
             CELL(IX2,IY2,2)=Y2
             CELL(IX2,IY2,3)=1
CT3
             print *,'Final position (',X2,',',Y2,')'
             TNDSKS=TNDSKS+1
             NDDEP=NDDEP+1
             ND = ND + 1
             IF (ND.EQ.50) THEN
                 WRITE(6,39010) NDDEP
                 ND = 0
             END IF
             IF (IHY.LT.(Y2+1)) THEN
                 IHY=Y2+1
             END IF
31002
        CONTINUE
31003
        WRITE(6,39011) NDDEP
        GO TO 01001
31004
        WRITE(6,39012) NDDEP
        GO TO 01001
C
```

```
C
C
                             TFG DEPOSITOR MESSAGES **
C
39000
        FORMAT(2X/, 'Number of disks to be deposited?
        FORMAT(15)
C39001
        FORMAT(2X/,'You are depositing more disks than there are cells i
39002
     Cn matrix!'/,'Please try again, but keep it under matrix max.')
        FORMAT(2X/,'What angle do you want it deposited at?
39003
C39004
        FORMAT (F7.4)
39005
        FORMAT(2X/,'Angle to large. Please try again.')
39006
        FORMAT(10(2X/), 'Deposition will occur at ',F8.4,' degrees, and w
     Cill deposit ',I5,' disks max.'/,4(2X/),10X,'D-Deposit as specified
     C'/,10X,'R-Reenter angle disk number'/,10X,'E?-Exit',5(2X/))
39007
        FORMAT (A2)
        FORMAT(2X/,'Incorrect response. Please try again.')
39008
39010
        FORMAT(I5,' disks deposited.')
        FORMAT(I5,' disks deposited -- DEPOSITON COMPLETED')
39011
        FORMAT('Spatail matrix full, deposition halted with ', I5,' disks
39012
     C deposited.')
C
cc
```

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CCC
                           MATRIX MANAGER
C
C
C
C
C
                 ****** MATRIX MANAGER INTERFACE LOOP
C
C
40001
        WRITE(6,49000)
40002
        READ(5,49002) CANS
        FLAG0=1
        IF (CANS.EQ.'RB') THEN
                GO TO 41000
        ELSE IF (CANS.EQ.'R') THEN
                GO TO 45000
        ELSE IF (CANS.EQ.'MA') THEN
                 GO TO 41000
        ELSE IF (CANS.EQ.'MD') THEN
                GO TO 42001
        ELSE IF (CANS.EQ.'W') THEN
                 GO TO 43000
        ELSE IF (CANS.EQ.'E') THEN
                 GO TO 01001
        ELSE IF (CANS.EQ.'EB') THEN
                GO TO 20001
        ELSE IF (CANS.EQ.'ED') THEN
                GO TO 30001
CT2,3
        ELSE IF (CANS.EQ.'EP') THEN
CT2,3
                 GO TO 50001
        ELSE IF (CANS.EQ.'EA') THEN
                 GO TO 60001
        ELSE IF (CANS.EQ.'MC') THEN
                 GO TO 44000
        ELSE IF (CANS.EQ.'WS') THEN
                 GO TO 46000
        ELSE IF (CAUS.EQ.'RS') THEN
                 GO TO 47000
        ELSE IF (CANS.EQ.'SA') THEN
                 GO TO 48100
        ELSE IF (CANS.EQ.'SB') THEN
                 GO TO 48200
        ELSE IF (CANS.EQ.'SC') THEN
                 GO TO 48300
        END IF
        WRITE(6,49001)
        GO TO 40002
C
```

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```
C
cc
                    ****** MATRIX READ BUFFER/ADD COMMAND ****
C
41000
        FLAG0=0
C
C
C
                   ****** MATRIX DELETE COMMAND *******
C
C
42001
        PAF=1
        IF (CANS.EQ.'RB') THEN
                 TNDSKS≈0
                 IHY=0
        END IF
        DO 42009 LENTRY=1,240
                 IF (NDSK(LENTRY).EQ.0) GO TO 42009
                 IF (NDSK(LENTRY).GT.1) GO TO 42003
                 IX=INT(DBUFF(1,LENTRY))
                 IY=INT(DBUFF(2,LENTRY))
                 IF (CELL(IX,IY,3).EQ.FLAGO) GO TO 42002
                 WRITE(6,49020) LENTRY
                 GO TO 40001
42002
                 IF (FLAGO.EQ.O) THEN
                         CELL(IX, IY, 1) = DBUFF(1, LENTRY)
                         CELL(IX, IY, 2) = DBUFF(2, LENTRY)
                         CELL(IX,IY,3)=1
                         IF (IX.LT.10) THEN
                                  XM=DBUFF(1,LENTRY)+XAXIS+1
                                  IXM = INT(XM)
                                  CELL(IXM,IY,1) = XM
                                  CELL(IXM, IY, 2) = DBUFF(2, LENTRY)
                                  CELL(IXM,IY,3)=1
                         END IF
                         TNDSKS=TNDSKS+1
                         IF (IHY.LT.IY) THEN
                                  IHY=IY
                         END IF
                 ELSE
                         CELL(IX,IY,1)=0
                         CELL(IX,IY,1)=0
                         CELL(IX,IY,3)=0
                         IF (IX.LT.10) THEN
                                  XM=DBUFF(1,LENTRY)+XAXIS+1
                                  IXM = INT(XM)
                                  CELL(IXM,IY,1)=0
                                  CELL(IXM,IY,2)=0
                                  CELL(IXM,IY,3) = 0
                         END IF
                         TNDSKS=TNDSKS-1
                          IF (IHY.GT.IY) THEN
                                  IHY=IY
                         END IF
```

```
END IF
                 PX=CELL(IX,IY,1)
                 PY=CELL(IX,IY,2)
                 print *,'Point entry at (',PX,',',PY,')'
CT2
                 PAF=0
                 GO TO 42009
                 RANGLE=DBUFF(3, LENTRY)/57.29577951
42003
                 IF (PAF.LT.1) GO TO 42004
                 PAH=PA+1.047197551
                 PAL=PA-1.047197551
                 IF (PAH.GE.6.283185307) THEN
                         PAH=PAH-6.283185307
                 END IF
                 IF (PAL.LT.0) THEN
                         PAL=PAL+6.283185307
                 END IF
                 IF ((RANGLE.GE.PAH).OR.(RANGLE.LE.PAL)) GO TO 42004
                 WRITE(6,49021) LENTRY
                 GO TO 40001
                 DO 42007 LSTEP=1,400
42004
                         X = PX + (LSTEP * 1.414213562 * COS(RANGLE))
                         Y=PY+(LSTEP*1.414213562*SIN(RANGLE))
                         IF (((X.GE.0).AND.(X.LE.XAXIS)).AND.((Y.GE.0).AN
     CD.(Y.LE.YAXIS))) GO TO 42005
                         WRITE(6,49022) LENTRY
                         GO TO 40001
                          IX = INT(X)
42005
                          IY = INT(Y)
                          IF (CELL(IX, IY, 3).EQ.FLAGO) GO TO 42006
                         WRITE(6,49020) LENTRY
                         GO TO 40001
42006
                          IF (FLAGO.EQ.O) THEN
                                  CELL(IX,IY,1) = X
                                  CELL(IX,IY,2) = Y
                                  CELL(IX,IY,3)=1
                                  IF (IX.LT.10) THEN
                                           XM=X+XAXIS+1
                                           IXM=INT(XM)
                                           CELL(IXM,IY,1) = XM
                                           CELL(IXM,IY,2) = Y
                                           CELL(IXM,IY,3)=1
                                  END IF
                                  TNDSKS=TNDSKS+1
                                  IF (IHY.LT.IY) THEN
                                           IHY=IY
                                  END IF
                          ELSE
                                  CELL(IX,IY,1)=0
                                  CELL(IX,IY,2)=0
                                  CELL(IX,IY,3)=0
                                  IF (IX.LT.10) THEN
                                           XM = X + XAXIS + 1
```

IXM = INT(XM)

```
CELL(IXM,IY,1)=0
                                          CELL(IXM,IY,2)=0
                                          CELL(IXM,IY,3)=0
                                  END IF
                                  TNDSKS=TNDSKS-1
                                  IF (IHY.GT.IY) THEN
                                          IHY=IY
                                  END IF
                         END IF
                         IF (NDSK(LENTRY).EQ.LSTEP) GO TO 42008
42007
                 CONTINUE
42008
                 PX = X
                 PY=Y
CT2
                 print *,'Line entry ending at (',PX,',',PY,')'
                 IF (RANGLE.LE.3.141592654) THEN
                         PA=RANGLE+3.141592654
                 ELSE
                         PA=RANGLE-3.141592654
                 END IF
42009
        CONTINUE
        GO TO 40001
C
C
C
                      ***** MATRIX WRITE FILE COMMAND **
C
C
        OPEN(3,FILE='dep',STATUS='NEW')
43000
        REWIND(3)
        WRITE(3,49030) XAXIS, YAXIS, IHY, TNDSKS
        CLOSE(3)
        OPEN(3,FILE='plot',STATUS='NEW')
        REWIND(3)
43003
        L=1
        DO 43005 J=XAXIS,0,-1
             DO 43004 \text{ K=YAXIS,0,-1}
                 IF (CELL(J,K,3).EQ.1) THEN
                     WBUFF(L,1) = CELL(J,K,1)
                     WBUFF(L,2) = CELL(J,K,2)
                     WBUFF(L,3) = SIZE
                     L=L+1
                     IF (L.EQ.6) THEN
                          WRITE(3,49033) ((WBUFF(M,N),N=1,3),M=5,1,-1)
                          L=1
                     END IF
                 END IF
                 IF ((J.EQ.0).AND.(K.EQ.0)) THEN
                     WRITE(3,49033) ((WBUFF(M,N),N=1,3),M=L,1,-1)
                 END IF
             CONTINUE
43004
43005
         CONTINUE
         CLOSE(3)
```

C

C

```
C
C
                    ****** MATRIX CLEAR COMMAND ******
C
C
44000
        CALL INITM (CELL, TNDSKS, IHY)
        GO TO 40001
C
Ċ
C
                 ****** MATRIX READ FILE COMMAND ******
C
C
45000
        OPEN(2,FILE='dep',STATUS='OLD')
        REWIND(2)
        READ(2,49030) XAXIS, YAXIS, IHY, TNDSKS
        CLOSE(2)
        OPEN(2,FILE='plot',STATUS='OLD')
        REWIND(2)
45001
        DO 45002 J=TNDSKS,1,-5
                 IF (J.LE.5) THEN
                         K⇒J
                 ELSE
                         K=5
                 END IF
                 READ (2,49033) (WBUFF (M,N), N=1,3), M=K,1,-1)
                 DO 45003 N=K,1,-1
                         IX=INT(WBUFF(N,1))
                         IY=INT(WBUFF(N,2))
                         CELL(IX,IY,1) = WBUFF(N,1)
                         CELL(IX, IY, 2) = WBUFF(N, 2)
                         CELL(IX,IY,3)=1
                         IF (WBUFF(N,1).LT.10) THEN
                                  XM=WBUFF(N,1)+XAXIS+1
                                  IXM = INT(XM)
                                  CELL(IXM,IY,1) = XM
                                  CELL(IXM,IY,2) = WBUFF(N,2)
                                  CELL(IXM,IY,3)=1
                         END IF
45003
                 CONTINUE
45002
        CONTINUE
        CLOSE(2)
        SIZE=WBUFF(N,3)
        GO TO 40001
```

```
C
                     ***** MATRIX WRITE SUBS FILE COMMAND ****
С
C
46000
       OPEN(3,FILE='subd',STATUS='NEW')
        REWIND(3)
       WRITE(3,49030) XAXIS, YAXIS, IHY, TNDSKS
        CLOSE(3)
        OPEN(3,FILE='subp',STATUS='NEW')
        REWIND(3)
        GO TO 43003
C
Ċ
č
                ****** MATRIX READ SUBS FILE COMMAND *****
C
C
47000
        OPEN(2,FILE='subd',STATUS='OLD')
        REWIND(2)
        READ(2,49030) XAXIS,YAXIS,IHY,TNDSKS
        CLOSE(2)
        OPEN(2,FILE='subp',STATUS='OLD')
        REWIND(2)
        GO TO 45001
C
Č
C
                ****** MATRIX SET AXES COMMAND *******
C
C
48100
        CALL INITM(CELL, TNDSKS, IHY)
        XAXIS=319
        YAXIS=239
        SIZE=0
        GO TO 40001
48200
        CALL INITM(CELL, TNDSKS, IHY)
        XAXIS=159
        YAXIS=119
        SIZE=.3
        GO TO 40001
48300
        CALL INITM (CELL, TNDSKS, IHY)
        XAXIS=79
        YAXIS=59
        SIZE=.7
        GO TO 40001
C
C
C
                C
49000
        FORMAT(2(2X/),25X,'MATRIX MANAGER',2(2X/),10X,'Set Axes'/,15X,'S
          320X240'/,15X,'SB 160X120'/,15X,'SC
                                                   80X60'/,10X,'Read Dat
     Ca Into Matrix From'/,15X,'R
                                    Plot and Dep Files'/,15X,'RB
```

```
Cer'/,15X,'RS
                     Subp and Subd Files '/,10X,'Write from Matrix to'/,
     C15X,'W
             Plot and Dep Files'/,15X,'WS Subp and Subd Files'/,10X
    C, 'Modify Matrix'/, 15X, 'MA Add Buffer Data to Matrix'/, 15X, 'MC
    CClear Matrix'/,15X,'MD Delete Buffer Data from Matrix'///,15X,'E
          Exit',2(2X/))
49001
        FORMAT(2X/,15X,'Incorrect response, please try agian.',2X)
49002
        FORMAT(A2,$)
49020
        FORMAT('Cell required by line ',I3,' is already filled/delet
     Ced. File aborted.')
        FORMAT('Angle required by line ',I3,' is to sharp.
                                                            File abo
     Crted.')
        FORMAT('Surface specified by line ', 13,' is out of matrix.
49022
     CFile aborted.')
49030
        FORMAT(13,2X,13,2X,15)
49033
        FORMAT(5(F6.2,1x,F6.2,1x,F2.1,1x),:)
49034
        FORMAT(5(F2.1,1x,F6.2,1x,F6.2,1x),:)
C
C
C
```

```
C
00000000
                         PRINT CELL CONTENT
C
                 ****** PRINT CELL CONTENT LOOP *******
c
C
CT2,350001
                 PRINT *, 'PRINT CELL CONTENT'
CT2,3
        L=0
CT2,3
        DO 50003 J=XAXIS,0,-1
CT2,3
                 DO 50002 K=YAXIS,0,-1
CT2,3
                         IF (CELL(J,K,3).EQ.1) THEN
CT2,3
                                  L=L+1
CT2,3
                                  PBUFFX(L) = CELL(J,K,1)
CT2,3
                                  PBUFFY(L) = CELL(J,K,2)
CT2,3
                         END IF
CT2,3
                         IF ((J.EQ.0).AND.(K.EQ.0)) THEN
CT2,3
                                  WRITE(6,59001) (PBUFFX(M), M=L,1,-1)
CT2,3
                                  WRITE(6,59001) (PBUFFY(M),M=L,1,-1)
CT2,3
                         ELSE IF (L.EQ.6) THEN
CT2,3
                                  WRITE(6,59000) (PBUFFX(M), M=L,1,-1), (PBU
CT2,3
          CFFY(N), N=L, 1, -1)
CT2,3
                                  L=0
                         END IF
CT2,3
CT2,350002
                         CONTINUE
CT2,350003
                 CONTINUE
CT2,350004
                 GO TO 01001
C
C
C
                 ******* PRINT CELL CONTENT MESSAGES *******
C
C
CT2,359000
                 FORMAT(6(F8.4,2X)/,6(F8.4,2X)/)
CT2,359001
                 FORMAT(6(F8.4,2X))
```

```
C
                             ANALYSIS
C
C
C
C
C
                   ****** ANALYSIS INTERFACE LOOP
C
60001
        WRITE(6,69000)
60002
        READ(5,69001) CANS
        IF (CANS.EQ.'D') THEN
                GO TO 60003
        ELSE IF (CANS.EQ.'A') THEN
                GO TO 60003
        ELSE IF (CANS.EQ.'E') THEN
                GO TO 01001
        ELSE IF (CANS.EQ.'EB') THEN
                GO TO 20001
        ELSE IF (CANS.EQ.'ED') THEN
                GO TO 30001
        ELSE IF (CANS.EQ.'EM') THEN
                GO TO 40001
CT2,3
        ELSE IF (CANS.EQ.'EP') THEN
CT2,3
                GO TO 50001
        END IF
        WRITE(6,69002)
        GO TO 60002
60003
        WRITE(6,69003) XAXIS, YAXIS, IHY
60004
        WRITE(6,69004)
        READ(5,69005) IANS1
        WRITE(6,69006)
        READ(5,69005) IANS2
        IF ((IANS1.GT.IANS2).AND.(IANS1.LT.(YAXIS+1)).AND.(IANS2.GE.0))
     CGO TO 61000
        WRITE(6,69007)
        GO TO 60004
C
C
C
                  ******* DENSITY ANALYSIS LOOP *******
C
C
61000
        DCNT=0
        CELCNT=0
        DO 61002 K=IANS1,0,-1
            DO 61001 J=XAXIS,0,-1
                 IF (CELL(J,K,3).EQ.1) THEN
                     DCNT=DCNT+1
                END IF
                CELCNT=CELCNT+1
```

```
61001
            CONTINUE
            IF (K.EO.IANS2) GO TO 61003
61002
        CONTINUE
61003
        DEN=DCNT/CELCNT
        WRITE(6,69010) DEN
        RDEN=DEN*1.732050808
        IF (CANS.EO.'D') GO TO 60001
C
C
C
                 ****** ANGLE ANALYSIS LOOP *******
C
C
62000
        IUY=IANS1
        ILY=IANS2
        MLEN=XAXIS+IUY-ILY-1
        DO 62013 M=0,89
            DIRIND(M) = 0
62013
        CONTINUE
        DO 62009 J=0,89
            ANG=J
            WRITE(6,69022) ANG
             RANG=ANG*.0174532925
            D=TAN(RANG)
            PNTR=0
             DO 62011 K=0,319
                 IF (K.GE.XAXIS) GO TO 62011
                 print *,'K =',K
CT4
                 DSKCNT=0
                 CELCNT=0
                 X=D*IUY+K
                 LX = X
                 DO 62008 IYS=IUY,0,-1
                     print *,'IUY=',IUY,'IYS=',IYS
CT4
                     X=D*IYS+K
                     ISHFT=(INT(X/(XAXIS+1)))*(XAXIS+1)
                     NXS = INT(X - ISHFT)
                     LXS=INT(LX-ISHFT)
                     DO 62007 IXS=LXS,0,-1
                          print *,'LXS=',LXS,'IXS=',IXS,'NXS=',NXS
CT4
                          IF (CELL(IXS, IYS, 3) . EQ.1) THEN
                              DSKCNT=DSKCNT+1
                              print *,'DSKCNT =',DSKCNT
CT4
                          END IF
                          IXS2=IXS+1
                          IF (CELL(IXS2, IYS, 3).EQ.1) THEN
                              DSKCNT=DSKCNT+1
                          END IF
                          CELCNT=CELCNT+2
                          print *,'CELCNT =',CELCNT
CT4
                          IF (CELCNT.GE.MLEN) GO TO 62012
                          IF (IXS.EQ.NXS) GO TO 62006
 62007
                     CONTINUE
                      LX = X
 62006
```

```
IF (IYS.LE.ILY) GO TO 62012
62008
                CONTINUE
62012
                DENLIN=((DSKCNT*1.732050808)/CELCNT)
                IF (DENLIN.LE.RDEN) THEN
                    S=((RDEN-DENLIN)/RDEN)**2
                ELSE
                    S=((DENLIN-RDEN)/(1-RDEN))**2
                END IF
CT4
                print *,'S =',S
                PNTR=PNTR+S
CT4
                print *,'PNTR =',PNTR
62011
            CONTINUE
62014
            DIRIND(J) = PNTR/(XAXIS+1)
62009
        CONTINUE
62010
        print *,'COMPLETE'
        OPEN(3, FILE='ans', STATUS='NEW')
        REWIND(3)
        WRITE(3,69020) (DIRIND(N), N=0,89)
        WRITE(3,69021) DEN,RDEN
        CLOSE(3)
        GO TO 60001
C
C
C
                  C
69000
        FORMAT(7(2X/),32X,'ANALYSIS PROGRAM'///,15X,'D-Density'/,15X,'A=
     CAngle'/,14X,'E?=Exit',7(2X/))
69001
        FORMAT (A2)
69002
        FORMAT(15X,'Incorrect response, please try again.'/)
69003
        FORMAT(12(2X/),32X,'ANALYSIS PROGRAM'//,5X,'Current matrix dime
     Cnsions are ',I3,'X',I3,'.'//,5X,'Current deposition height is ',I3
     C,'.'///)
69004
        FORMAT(5X,'What do you want the analysis upper bound to be? '$)
69005
        FORMAT(13)
69006
        FORMAT(/5X,'What do you want the analysis lower bound to be? '$)
69007
        FORMAT(/5X,'Improper boundary conditions. Please try again.')
69010
        FORMAT('Density is ',F7.4,'disks per square unit')
69020
        FORMAT(9(10(F7.6,1X),/))
        FORMAT(F12.8,1X,F12.8)
69021
69022
        FORMAT('Angle ',F4.1)
C
```

```
C
C
C
C
                              ERROR TRAP
C
C
C
C
Č
C
                             DEPOSITION LOOP *****
C
C
CT380000
                     print *,'RAND=',RAND
C
C
C
                    --- COLLISION POINT DETERMINATION -----
C
C
CT3
             Y2 = 0
CT3
             DO 81205 ISTEP=0,3
CT3
                 print *,'ISTEP=',ISTEP
CT3
                 AA=RAND+1.414592654/CA
CT3
                 AS = RAND + .9428090416 * (ISTEP/CA)
CT3
                 X=D*IHY+AS
CT3
                 JUMP = 0
CT3
                 LX=X
                 DO 81204 IYS=IHY,0,-1
CT3
CT3
                      print *,'IHY=',IHY,' IYS=',IYS
CT3
                      X=D*IYS+AS
CT3
                      ISHFT=(INT(x/(XAXIS+1)))*(XAXIS+1)
CT3
                      NXS = INT(X - ISHFT)
CT3
                      LXS=INT(LX-ISHFT)
CT3
                      DO 81202 IXS=LXS,0,-1
CT3
                          print *,'LXS=',LXS,'IXS=',IXS,'NXS=',NXS
CT3
                          IF (CELL(IXS, IYS, 3).EQ.1) THEN
CT3
                              IF ((IXS.EQ.IXT).AND.(IYS.EQ.IYT)) GO TO 812
CT3
         C07
CT3
                              XMIN=D*CELL(IXS,IYS,2)+RAND-ISHFT
CT3
                              XMAX=XMIN+2.828427125/CA
                              print *,'Possible Cl (',CELL(IXS,IYS,1),',',
CT3
                              XMIN=',XMIN,'
CT3
         CCELL(IXS, IYS, 2),')
                                               XMAX=',XMAX
CT3
                               IF (ISTEP.LT.2) THEN
CT3
                                   IF ((CELL(IXS, IYS, 1).LT.XMIN).OR.(CELL(I
CT3
         CXS, IYS, 1).GT.XMAX)) GO TO 81207
                                   A=AA-ISHFT
CT3
CT3
                                   F=CELL(IXS, IYS, 2) -D*(A-CELL(IXS, IYS, 1))
CT3
                                   G=(A-CELL(IXS, IYS, 1))+D*CELL(IXS, IYS, 2)
CT3
                                   Y=(F+SORT(2*E-G*G))/E
CT3
                                   print *,'Y coord ',Y
CT3
                                   IXT=IXS
CT3
                                   IYT=IYS
CT3
                                   IF (Y2.LT.Y) THEN
```

```
CT3
                                      Y2=Y
CT3
                                       IX1=IXS
CT3
                                      IY1=IYS
CT3
                                       A2=A
CT3
                                  END IF
CT3
                                  JUMP=1
CT3
                              ELSE
CT3
                                  IF ((CELL(IXS, IYS, 1).LT.XMIN).OR.(CELL(I
CT3
        CXS, IYS, 1).GT.XMAX)) GO TO 81207
CT3
                                  A=AA-ISHFT
CT3
                                  F=CELL(IXS, IYS, 2) -D*(A-CELL(IXS, IYS, 1))
CT3
                                  G=(A-CELL(IXS,IYS,1))+D*CELL(IXS,IYS,2)
CT3
                                  Y=(F+SQRT(2*E-G*G))/E
CT3
                                  print *,'Y Coord ',Y
CT3
                                  IXT=IXS
CT3
                                  IYT=IYS
                                  IF (Y2.LT.Y) THEN
CT3
CT3
                                       Y2=Y
CT3
                                       IX1=IXS
CT3
                                       IY1=IYS
CT3
                                       A2=A
CT3
                                  END IF
CT3
                                  JUMP=1
                              END IF
CT3
CT3
                         END IF
CT381207
                                  IF (IXS.EQ.NXS) GO TO 81206
CT381202
                              CONTINUE
CT381206
                              LX≠X
CT3
                     IF (JUMP.EQ.1) GO TO 81205
CT381204
                         CONTINUE
CT381205
                CONTINUE
CT3
             X2=D*Y2+A2
            print *,'X2 before shift=',X2
CT3
CT3
             IF (IX1.LT.3) THEN
CT3
                 X2=X2+XAXIS+1
CT3
                 IX1=IX1+XAXIS+1
CT3
CT3
            print *,'Cl (',IX1,',',IY1,') X2=',X2,'Y2=',Y2
C
C
C
                    --- REST POINT DETERMINATION ----
C
C
C
CT381300
                     SHORT=18
             DO 81302 J=-3,3
CT3
CT3
                 IX3=J+IX1
CT3
                 DO 81301 K=-3.3
CT3
                     IY3=K+IY1
CT3
                     IF ((IY3.LT.0).OR.(IYS.GT.IHY)) GO TO 81301
CT3
                     IF (CELL(IX3,IY3,3).EQ.1) THEN
CT3
                          print *,'Possible Rest Cell (',IX3,',',IY3,')'
CT3
                          X31=CELL(IX3,IY3,1)-CELL(IX1,IY1,1)
```

```
CT3
                          Y31=CELL(IX3,IY3,2)-CELL(IX1,IY1,2)
CT3
                          R13SQR = (X31**2) + (Y31**2)
CT3
                          print *,CELL(IX3,IY3,1),CELL(IX1,IY1,1),CELL(
CT3
        CIX3, IY3, 2), CELL(IX1, IY1, 2)
                          print *,'R13SQR=',R13SQR
CT3
CT3
                          IF ((R13SQR.GE.1.8).AND.(R13SQR.LE.8.0)) THEN
CT3
                               R=R13SQR
                               STX = (X31**2)*(R*R)-R*((R*R)-8*(Y31**2))
CT3
CT3
                               IF (STX.LT.0) THEN
CT3
                                   TX = 0
CT3
                               ELSE
                                   TX=SQRT(STX)
CT3
                               END IF
CT3
                               STY = (Y31**2)*(R*R)-R*((R*R)-8*(X31**2))
CT3
CT3
                               IF (STY.LT.0) THEN
CT3
                                   TY=0
CT3
                               ELSE
CT3
                                   TY=SQRT(STY)
CT3
                               END IF
CT3
                               DO 81303 L=-1,1,2
CT3
                                   IF (X31.GE.O) THEN
CT3
                                       X2T = (X31*R+L*TX)/(2*R)
CT3
                                   ELSE
CT3
                                       X2T = (X31*R-L*TX)/(2*R)
CT3
                                   END IF
CT3
                                   IF (Y31.LE.O) THEN
                                        Y2T = (Y31*R+L*TY)/(2*R)
CT3
                                   ELSE
CT3
                                        Y2T = (Y31*R-L*TY)/(2*R)
CT3
CT3
                                   END IF
CT3
                                   X22=X2T+CELL(IX1,IY1,1)-X2
CT3
                                   Y22=Y2T+CELL(IX1,IY1,2)-Y2
CT3
                                   R22SQR = (X22**2) + (Y22**2)
                                   print *,'R22SQR=',R22SQR
CT3
CT3
                                   IF (R22SQR.LT.SHORT) THEN
CT3
                                        SHORT=R22SQR
                                       print *,'SHORT=',SHORT
CT3
CT3
                                       X2F=X2T
CT3
                                        Y2F=Y2T
CT3
                                        IX3F = IX3
CT3
                                        IY3F=IY3
CT3
                                        FX31=X31
CT3
                                        FY31=Y31
CT3
                                        FR13SQ=R13SQR
CT3
                                   END IF
                                        CONTINUE
CT381303
CT3
                          END IF
CT3
                      END IF
CT381301
                          CONTINUE
CT381302
                      CONTINUE
CT3
             R13=SQRT(FR13SQ)
CT3
             print *,'Rl3=',Rl3
```

CT3

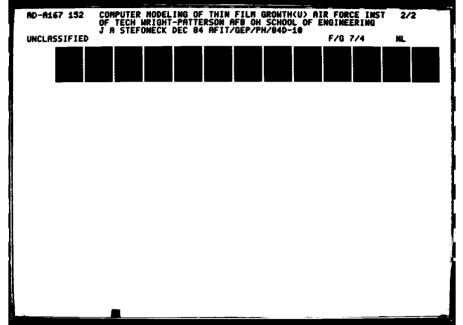
X21=X2F

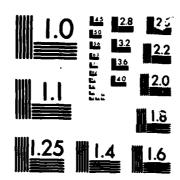
```
CT3
            Y21=Y2F
CT3
            R12SQR=X21**2+Y21**2
            X2=X2F+CELL(IX1,IY1,1)
CT3
CT3
            Y2=Y2F+CELL(IX1,IY1,2)
CT3
            print *,'X2=',X2,'Y2=',Y2
CT3
            IX2 = INT(X2)
CT3
            IY2 = INT(Y2)
CT3
            X23=X2-CELL(IX3F,IY3F,1)
CT3
            Y23=Y2-CELL(IX3F,IY3F,2)
CT3
            R23SQR=X23**2+Y23**2
CT3
            IF (IX2.GT.XAXIS) THEN
CT3
                 X2=X2-(XAXIS+1)
CT3
            END IF
            print *,'Final position (',X2,',',Y2,')'
CT3
CT3
            print *,'OVERWRITE ERROR--PROGRAM HALTED(',NDDEP,')'
99999
        END
C
C
```

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```
C
0000000
                          SYSTEM SUBROUTINES
C
         SUBROUTINE INITB (DBUFF, NDSK)
         INTEGER NDSK(240)
         REAL DBUFF(3,240)
00030
         DO 00032 L=1.3
                 DO 00031 LL=1,240
                          DBUFF(L,LL)=0
00031
                 CONTINUE
00032
         CONTINUE
         DO 00033 L=1,240
                  NDSK(L) = 0
00033
         CONTINUE
         END
C
C
         SUBROUTINE INITM(CELL, TNDSKS, IHY)
         REAL CELL(0:329,0:239,3)
00034
         DO 00037 L=0,329
                  DO 00036 LL=0,239
                          CELL(L,LL,3)=0
00036
                 CONTINUE
00037
         CONTINUE
         TNDSKS=0
         IHY=0
         END
C
```





MICROCOPY

CHART

Appendix B

Derivation

Incident Disk Coordinates After Collision

The incident disk coordinates after collision are used by the collision point determination algorythm discussed in Section V. The formulas for these coordinates are used in the TFG Simulator and are derived here (See Appendix A for the coded routine and Figure 3.10 for a diagram).

Y Coordinate. The equation of a line in the slope interecept form is:

$$X = \frac{1}{m}Y + a$$

where

m = slope

a = x intercept

Also, the equation for a circle is:

$$r^2 = (x-h)^2 + (y-k)^2$$

where

h = x coordinate of circle center

k = y coordinate of circle center

r = cicle radius,

To find the y coordinate, X from the slope intercept equation is substitued into the X from the circle equation and solved for Y.

$$r^2 = (Y/m + a - h)^2 + (Y - k)^2$$

Expanding and putting in the quadradic form

$$(1/m^2 + 1)Y^2 + 2[(a-h)/m - k]Y + (a-h)^2 + k^2 - r^2 = 0.$$

Solving this for Y

$$Y = \frac{-(\frac{(a-h)}{m} - k) + \sqrt{r^2(\frac{1}{m^2} + 1) - ((a-h) + \frac{k}{m})^2}}{(\frac{1}{m^2} + 1)}.$$

 \underline{X} Coordinate. Since the value for Y is determined first, the X value can now be determined from

$$X = Y/m + a$$
.

Incident Disk Rest Point Coordinates

The incident disk rest point coordinates are used by the roll and rest point determination algorythm discussed in Section V. The formulas for these coordinates are used in the TFG Simulator and are derived here (See Appendix A for the coded routine and Figure 3.11 for a diagram).

 \underline{X} Coordinate. Given points P' and P" the line A passing through them can be written as:

$$\frac{X - X_H}{A - X_H} = \frac{X_I - X_H}{A - X_H}$$

However, in this case X''=0 and Y''=0. So the equation becomes Y = Y'X/X'.

Since B is perpendicular to A

slope of
$$B = -1/m$$
.

Also, since $X^{n}=0$ and $Y^{n}=0$ the intersection of A and B is at

$$X_C = X^{\dagger}/2$$
 and $Y_C = Y^{\dagger}/2$.

With this the equation for line B becomes

$$X - Y_C = -(X - X_C).$$

Substituting and reorganizing

$$Y = -\frac{X^{i}}{Y^{i}}X + \frac{X^{i}^{2}}{2Y^{i}} + \frac{Y^{i}}{2}.$$
 (1)

or

$$X = -\frac{Y'}{X'}Y + \frac{Y'^2}{2X'} + \frac{X'}{2}.$$
 (2)

Since the center of C lies on B and circle C", the y coordinate for the C center can now be found by substituting the Y above into the equation for circle C".

$$C'' = Y^{2} + X^{2} = 2$$

$$C'' = \left(\frac{-X^{i}}{Y^{i}}X + \frac{X^{i}^{2}}{2Y^{i}} + \frac{Y^{i}}{2}\right)^{2} + X^{2} = 2$$
(3)

Expanding and putting into quadratic form

$$X^{2}[4R] - X[4X'R] + [R^{2} - 8Y'^{2}] = 0$$

where

$$R = (X^{12} + Y^{12}).$$

Solving this for X using the quadratic formula

$$X = \frac{X'R \pm \sqrt{X'^2R^2 - R(R^2 - 8Y'^2)}}{2R}.$$

By working with this equation for X, it soon becomes apparent that the plus is used when X' is greater than zero.

 \underline{Y} Coordinate. The y coordinate is determined similarly by substituting X from equation 2 into equation 3. The resulting equation is

$$Y = \frac{Y'R \pm \sqrt{Y'^2R^2 - R(R^2 - 8X'^2)}}{2R}$$

By working with this equation for Y, it soon becomes apparent that the plus is used when Y' is less than zero.

Density Definitions and Derivations

The density defintions and derivations presented here are used in the analysis portion of the TFG Simulator and

discussed in Section V. The actual coded routines are presented in Appendix A.

The density of any given computer generated material is defined as

DEN = DSKCNT/CELCNT

where

DSKCNT = number of disks CELCNT = number of cells.

Consequently, the absolute density is defined as follows:

ADEN = (total disk area)/(total film area)

=[DSKCNTx (area/disk)]/[CELCNT x (area/cell)].

However,

area/disk = $\pi R^2 = \pi (\sqrt{2}/2)^2 = \pi/2$

and

area/cell = 1.

Therefore,

ADEN = $(\Pi/2)$ x DEN = $(\Pi \times DSKCNT)/(2 \times CELCNT)$.

In addition, the maximum absolute density can be determined by considering the absolute density of a hexagonal close pack substance. Maximum absolute density is

where

DSKCNT x (area/disk) = $3\Pi/2$ CELCNT x (area/cell) = hexagonal area = $3\sqrt{3}$.

Therefore, the maximum absolute density is

MADEN = $\pi T/(2\sqrt{3})$.

Finally, the relative density is defined as

RDEN = ADEN/MADEN = $\sqrt{3}$ x DEN

where

ADEN = $(\Pi \times DSKCNT)/(2 \times CELCNT)$ MADEN = $\Pi/(2/3)$.

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Captain Jeffrey A. Stefoneck was born on 25 November 1951 in Rhinelander, Wisconsin. He graduated from Rhinelander High School in 1970 and then attended the University of Wisconsin from which he received the degree of Bachelor of Science in Physics in May 1974. Upon graduation, he received a commission in the USAF through the ROTC program and was called to active duty in October 1974. He completed Missile Combat Crew Readiness training and then served four years with the 90th Strategic Missile Wing as a missile combat crew member, F.E. Warren AFB, Wyoming. While at F.E. Warren AFB, he completed a variety of courses in Business Management and Electrical Engineering from the University of Wyoming and Colorado State University respectively. In March of 1979 he attended the School of Systems and Logistics, Air Force Institute of Technology (AFIT). After completion of the Systems Acquisition Short Course he worked with the Strategic Communications Systems Program Offices, Electronic Systems Division, Hanscom AFB, Massachusetts, until entering the School of Engineering, AFIT, in May 1983.

Permanent address: 1140 N. Stevens St

Rhinelander, Wisconsin 5450

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A two dimensional, hard disk computer model has been made which simulates thin film growth. The model represents deposition molecules by hard disks, which are trajected at some angle to the substrate. At the substrate, the model assumes a limited mobility where incident molecules are captured upon contact and then allowed to move to the nearest rest pocket. The model monitors disk movement by organizing the deposition field into a 320 by 240 array.

An analysis of nine different deposition angles shows that structural anisotropy and voids are a natural occurrence of the deposition process. The amount of unfilled space and the anisotropy can be linked to the deposition angle and mobility of the incident particles.

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